

Balanced Stages

Balancing of two-terminal devices

Odd function synthesis with anti-series and complementary series connection

Element relation:

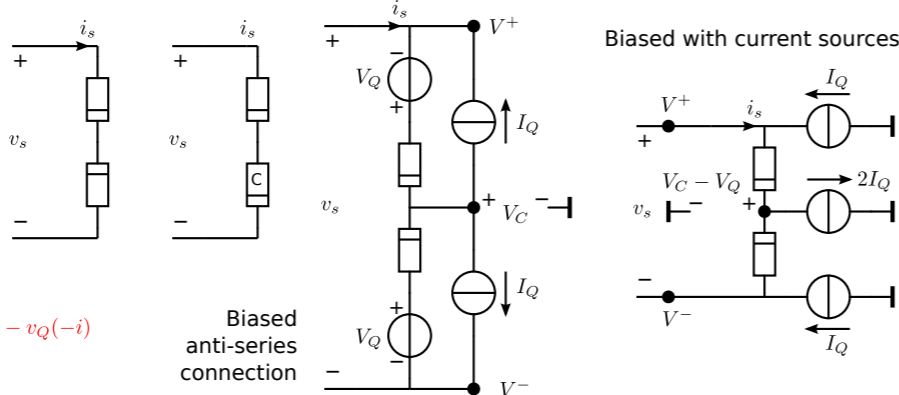
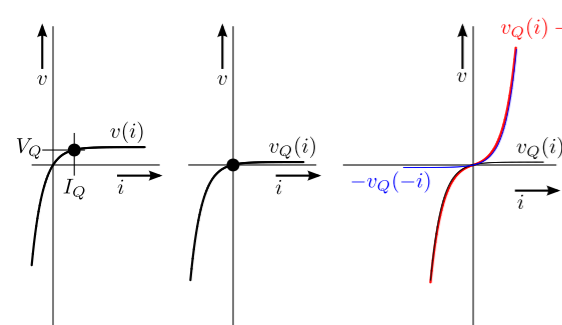
$$v(i) = a_0 + a_1 i + a_2 i^2 + a_3 i^3 + \dots$$

Balancing technique with series connection:

$$v_s = v(i_s) - v(-i_s)$$

Circuit synthesis

- anti-series connection of equal elements
- series connection of complementary elements



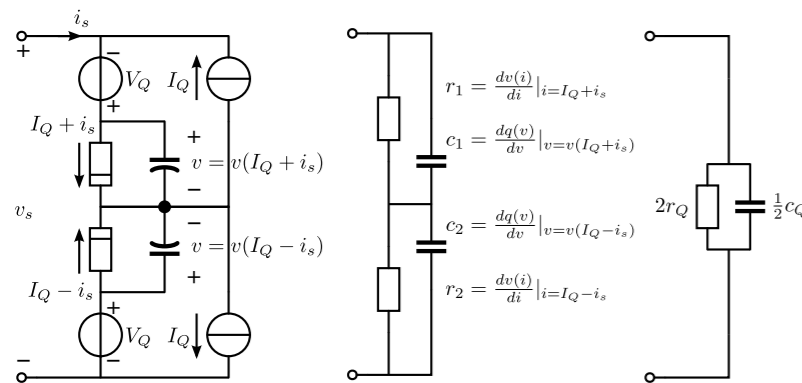
Differential-mode: odd transfer

$$v_s = v(i_s) - v(-i_s) = +a_0 + a_1 i_s + a_2 i_s^2 + a_3 i_s^3 + \dots - a_0 + a_1 i_s - a_2 i_s^2 + a_3 i_s^3 - \dots = 2(a_1 i_s + a_3 i_s^3 + \dots)$$

Common-mode: even transfer

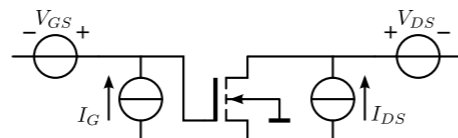
$$v_{cm} = \frac{1}{2}(v(i_s) + v(-i_s)) = \frac{1}{2}(+a_0 + a_1 i_s + a_2 i_s^2 + a_3 i_s^3 + \dots + a_0 - a_1 i_s + a_2 i_s^2 - a_3 i_s^3 + \dots) = a_0 + a_2 i_s^2 + \dots$$

Small-signal equivalent circuit



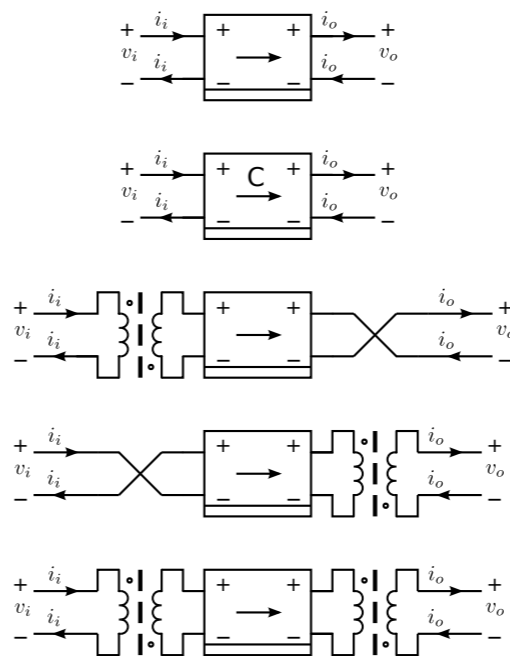
Noise

In quiescent operating point: Voltage noise spectrum twice that of the single element



Balancing of two-ports

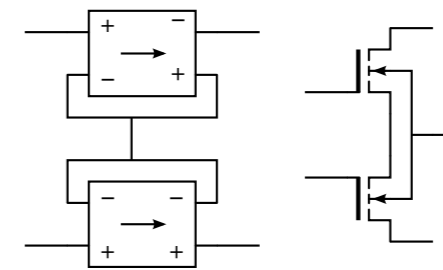
Two-ports and complementary two-ports



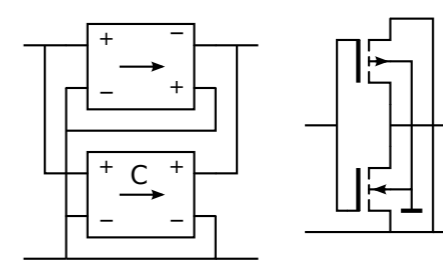
Eight possible interconnections with odd transfer

Two possible connections with three-terminal devices

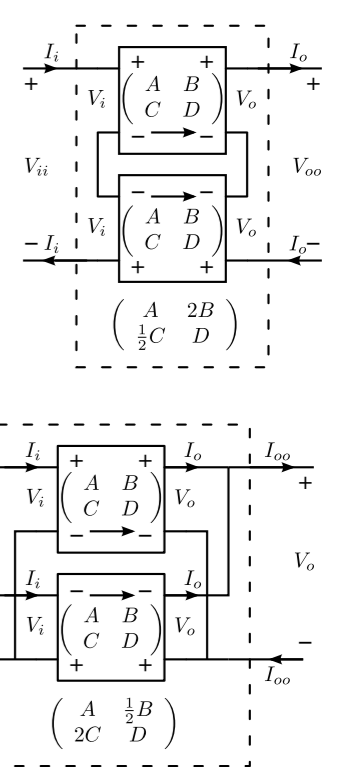
Anti-series connection of equal devices



Parallel connection of complementary devices



Small-signal models



Odd function synthesis with anti-parallel and complementary parallel connection

Element relation:

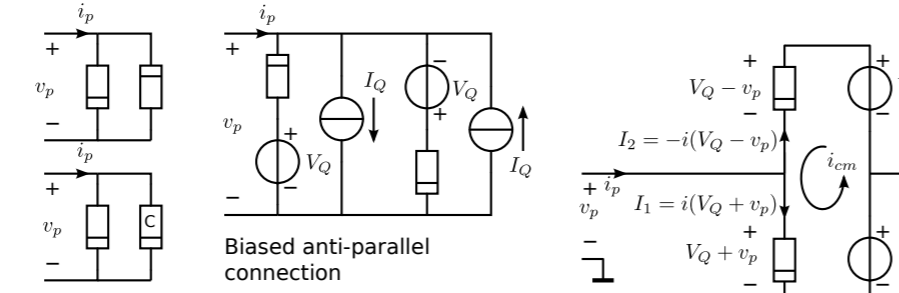
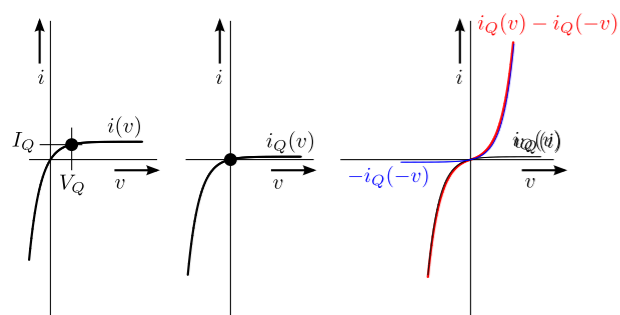
$$i(v) = a_0 + a_1 v + a_2 v^2 + a_3 v^3 + \dots$$

Balancing technique with parallel connection:

$$i_p = i(v_p) - i(-v_p)$$

Circuit synthesis

- anti-parallel connection of equal elements
- parallel connection of complementary elements



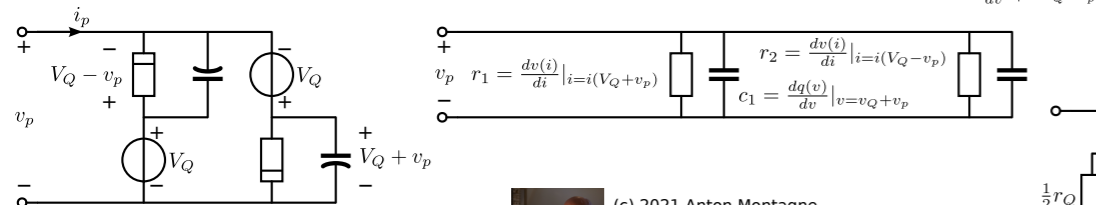
Differential-mode: odd transfer

$$i_p = i(v_p) - i(-v_p) = +a_0 + a_1 v_p + a_2 v_p^2 + a_3 v_p^3 + \dots - a_0 + a_1 v_p - a_2 v_p^2 + a_3 v_p^3 - \dots = 2(a_1 v_p + a_3 v_p^3 + \dots)$$

Common-mode: even transfer

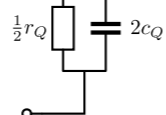
$$i_{cm} = \frac{1}{2}(i(v_p) + i(-v_p)) = \frac{1}{2}(+a_0 + a_1 v_p + a_2 v_p^2 + a_3 v_p^3 + \dots + a_0 - a_1 v_p + a_2 v_p^2 - a_3 v_p^3 + \dots) = a_0 + a_2 v_p^2 + \dots$$

Small-signal equivalent circuit

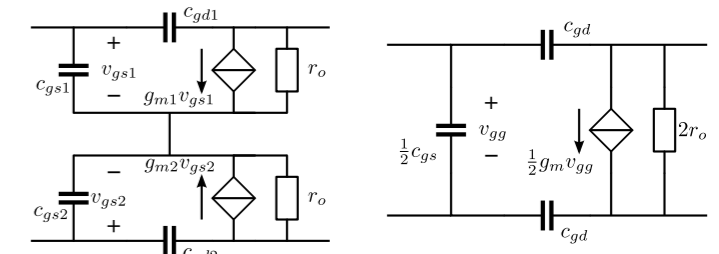
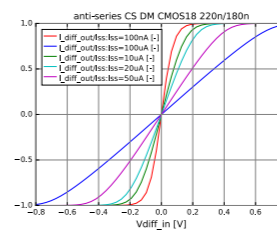
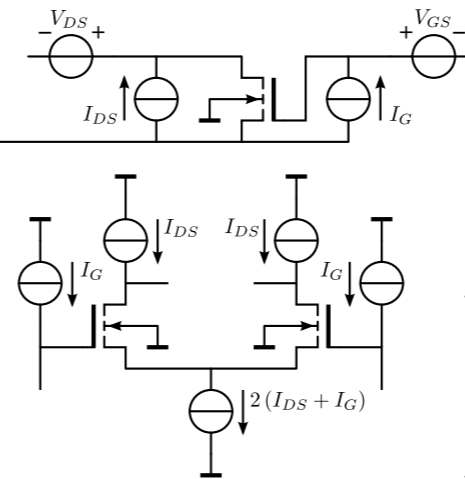


Noise

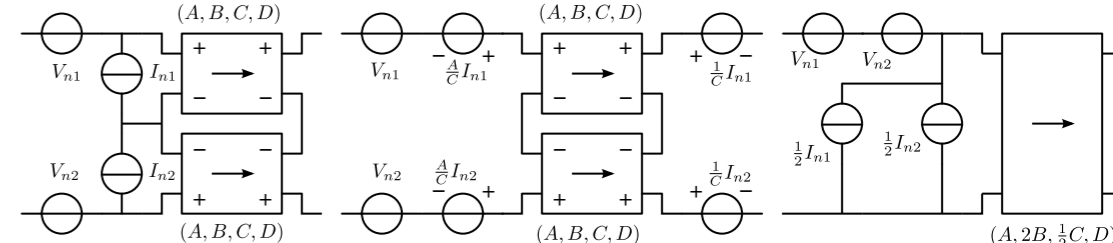
In quiescent operating point: Current noise spectrum twice that of the single element



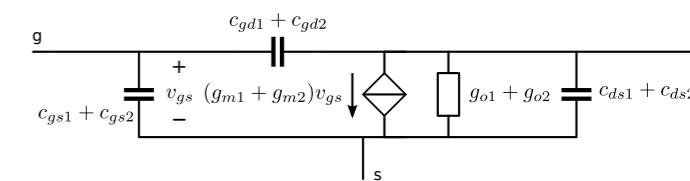
Anti-series stage



Noise

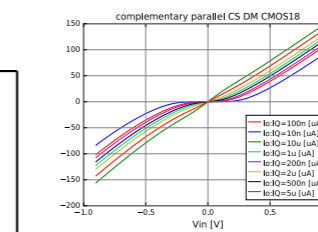
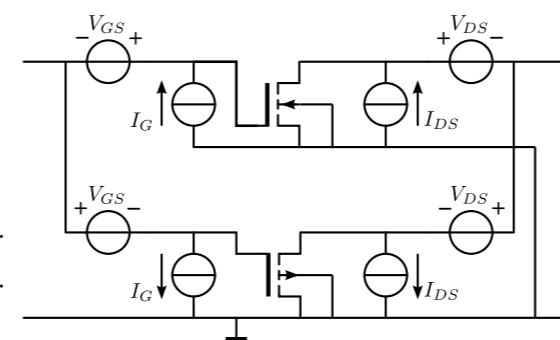


In quiescent operating point: Voltage noise spectrum twice that of the single element, current noise spectrum half of that of the single element



In quiescent operating point: Current noise spectrum twice that of the single element, voltage noise spectrum half of that of the single element

Complementary-parallel stage



Noise

