

Structured Electronic Design

EE3C11

Amplifiers: Modeling of Ideal Behavior

Anton J.M. Montagne

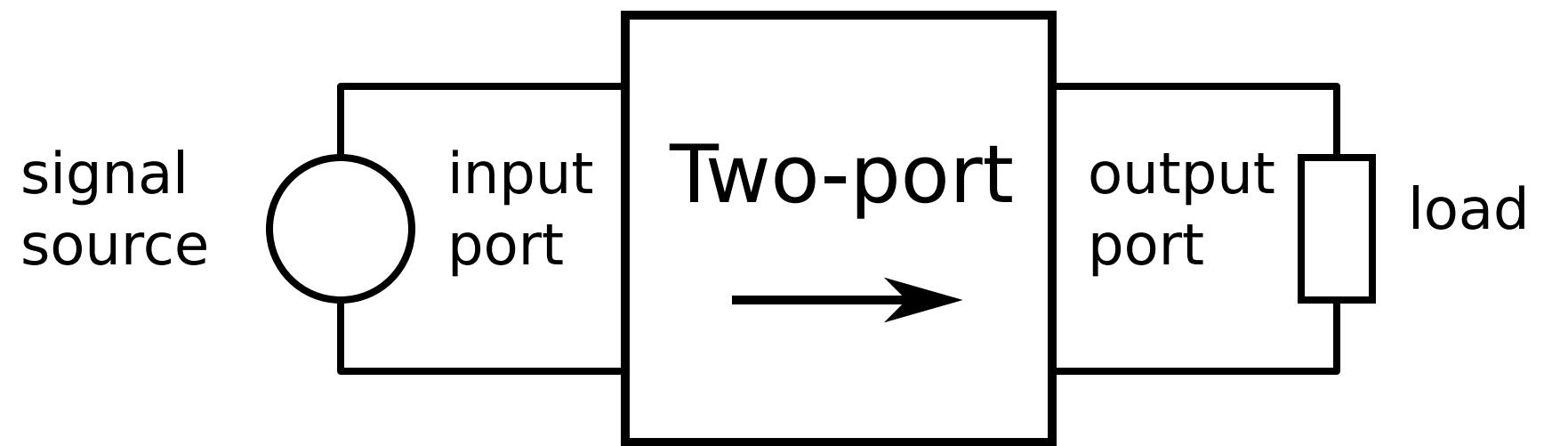
Two-port model

Two-port model

Functional model:
the power port will be omitted

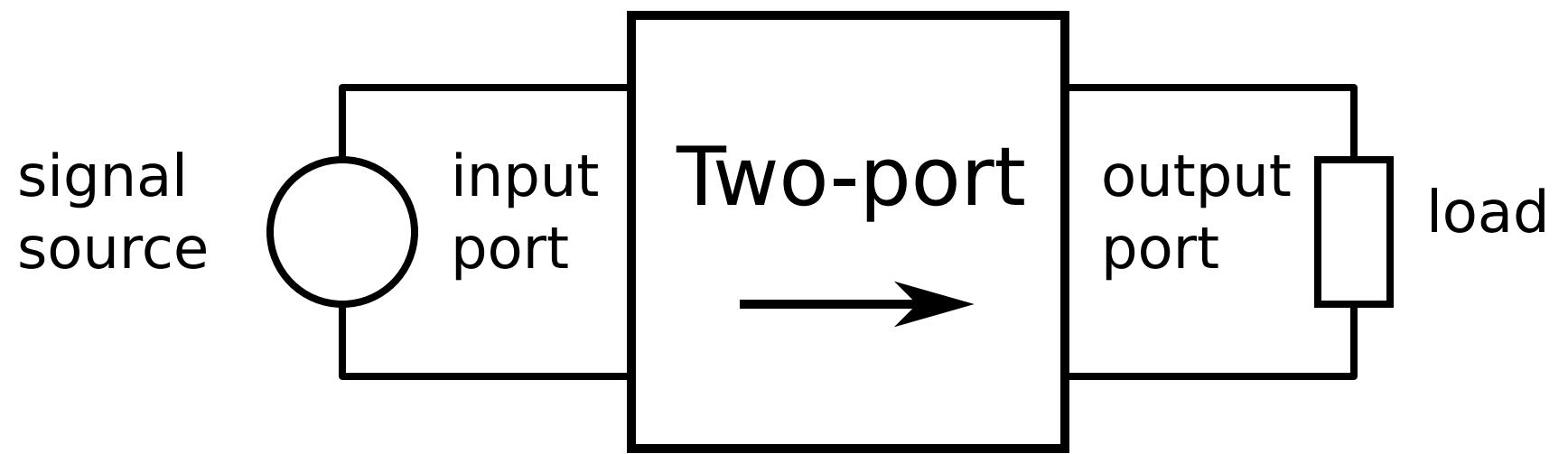
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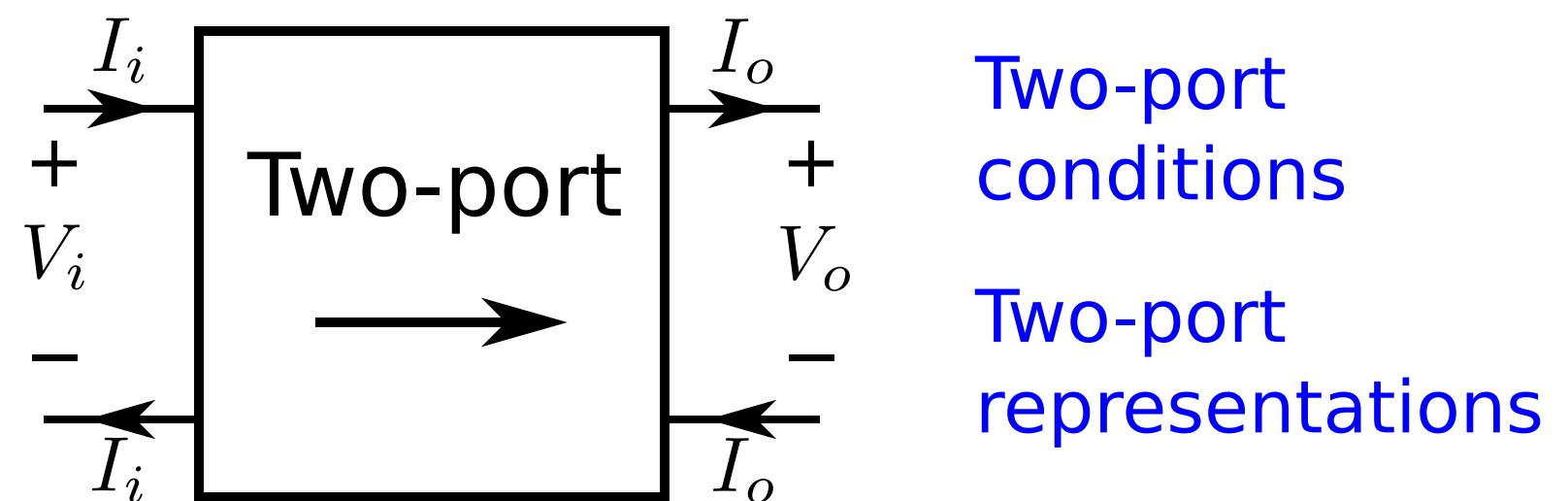


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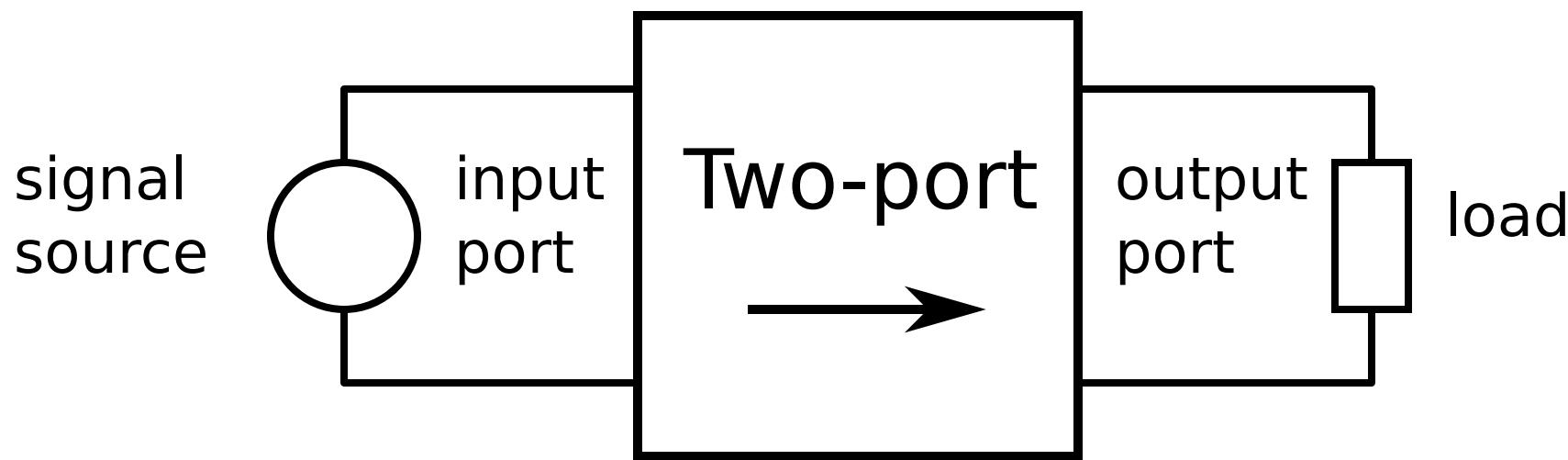
Two-port modeling: Chapter 18.6



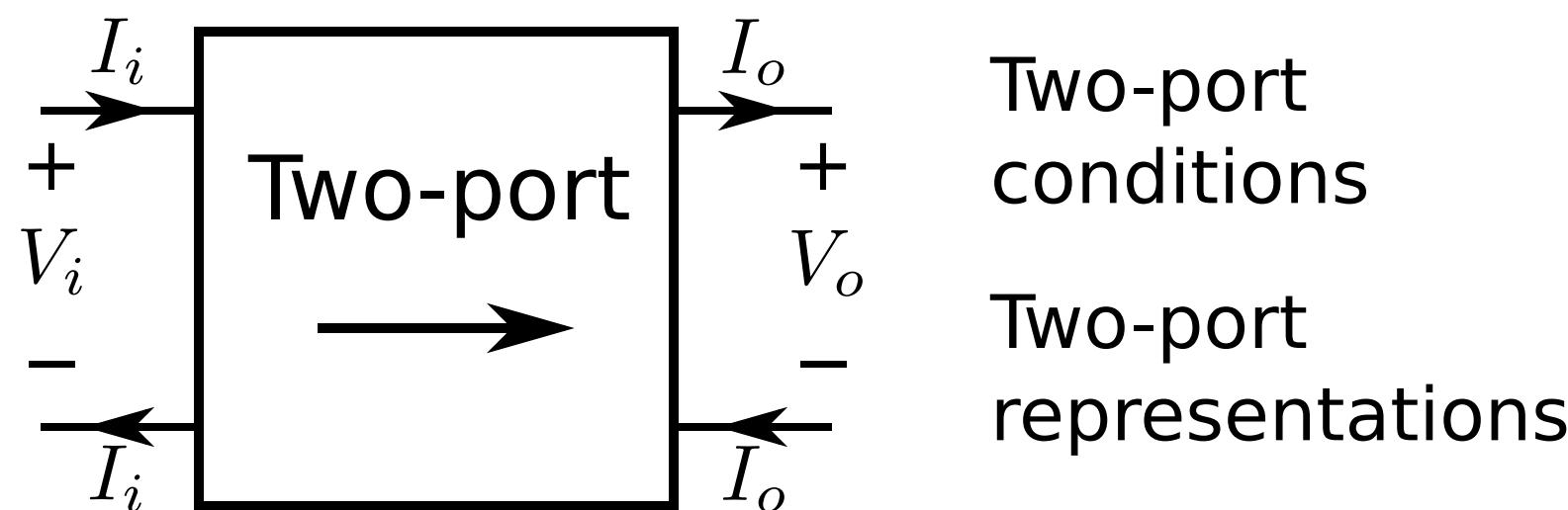
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Transmission-1 (anti-causal)
representation



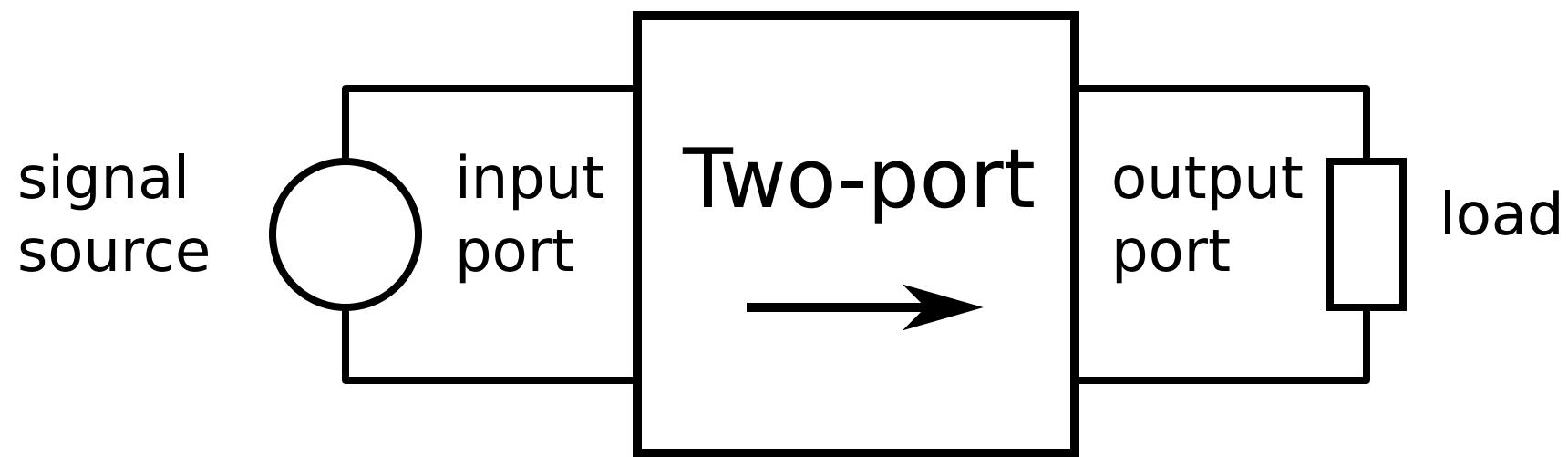
Two-port modeling: Chapter 18.6



Two-port model

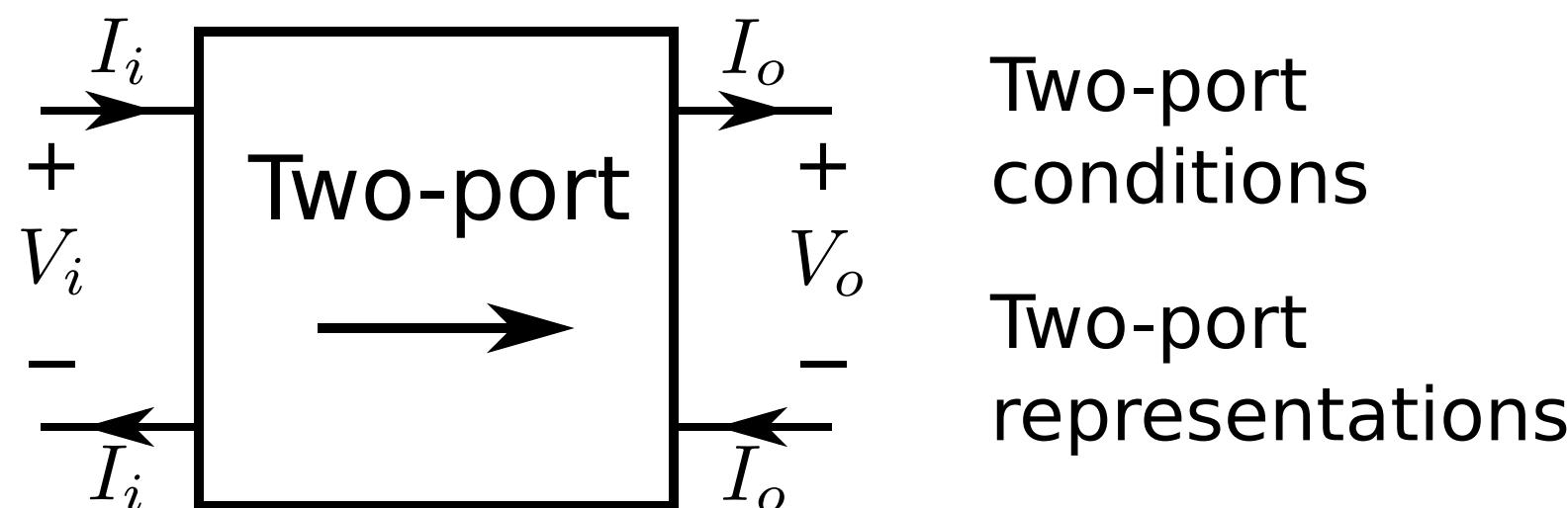
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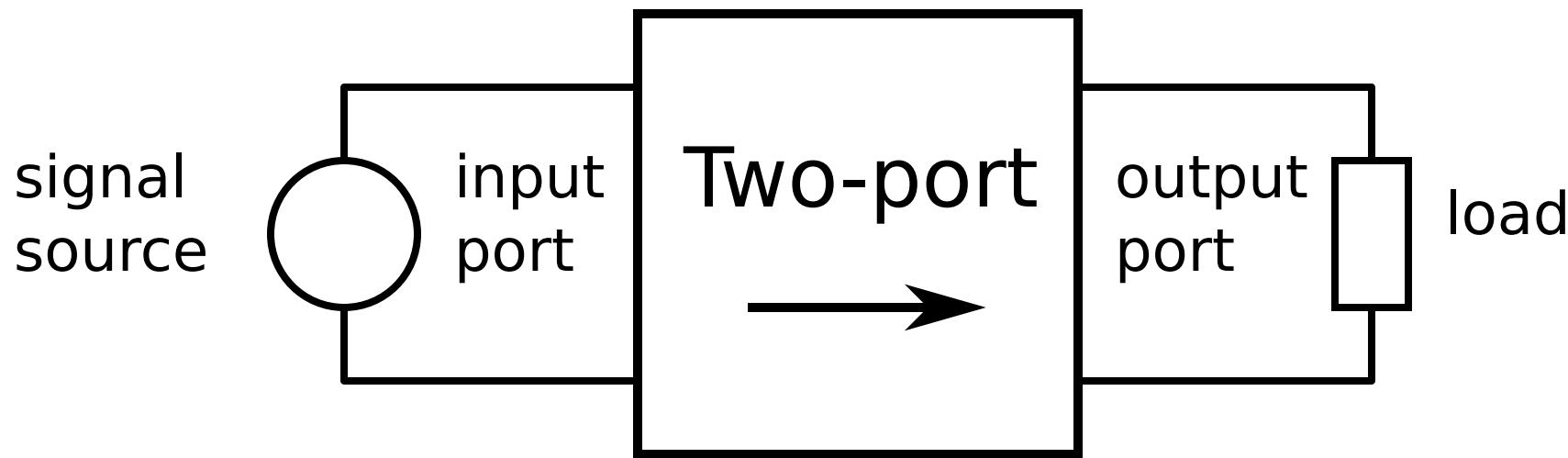
$$\begin{pmatrix} V_i \\ I_i \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} V_o \\ I_o \end{pmatrix}$$

Two-port modeling: Chapter 18.6



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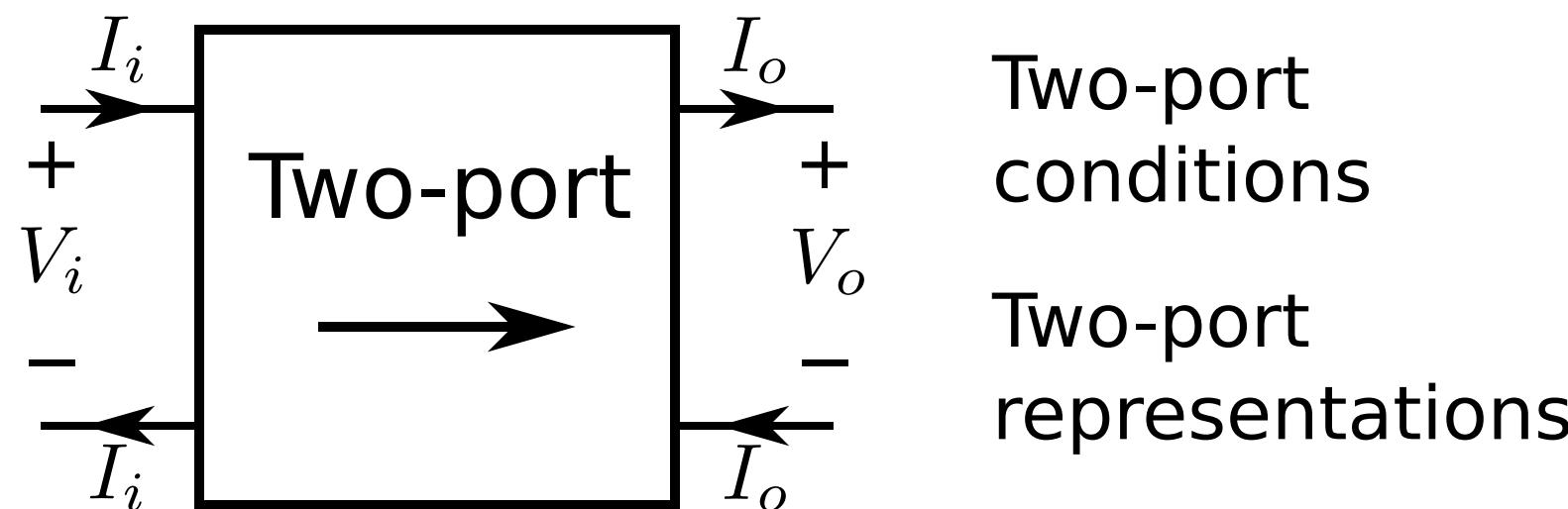
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$$\begin{pmatrix} V_i \\ I_i \end{pmatrix} = \begin{pmatrix} A & B \\ C & D \end{pmatrix} \begin{pmatrix} V_o \\ I_o \end{pmatrix}$$

$$A = \frac{1}{\mu} = \left. \frac{V_i}{V_o} \right|_{I_o=0},$$

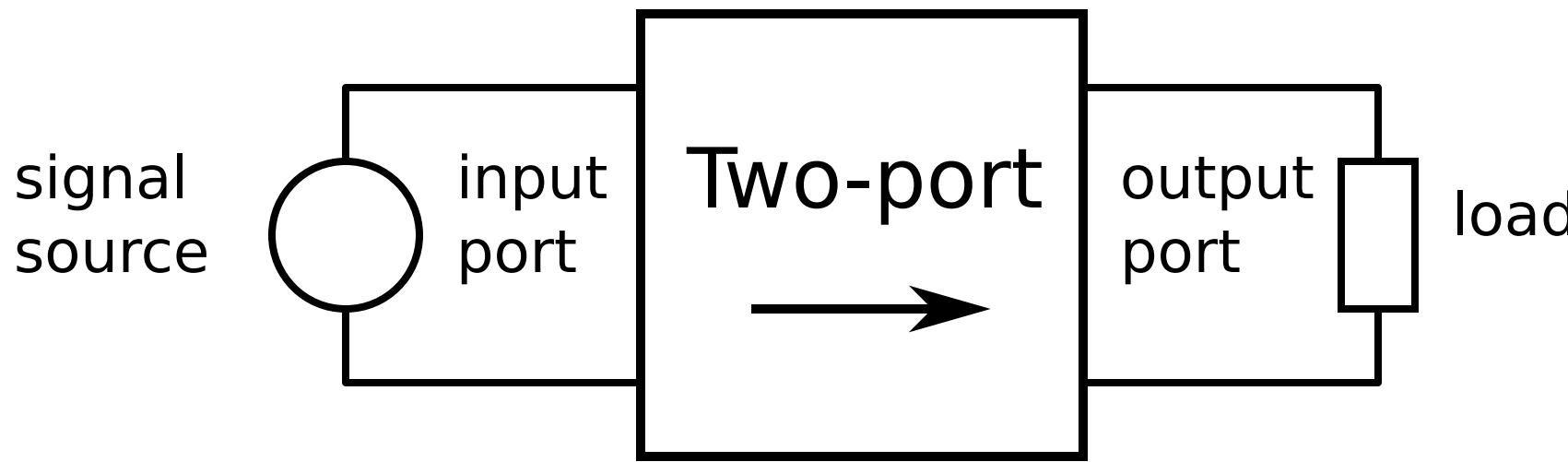
Open output

Two-port modeling: Chapter 18.6



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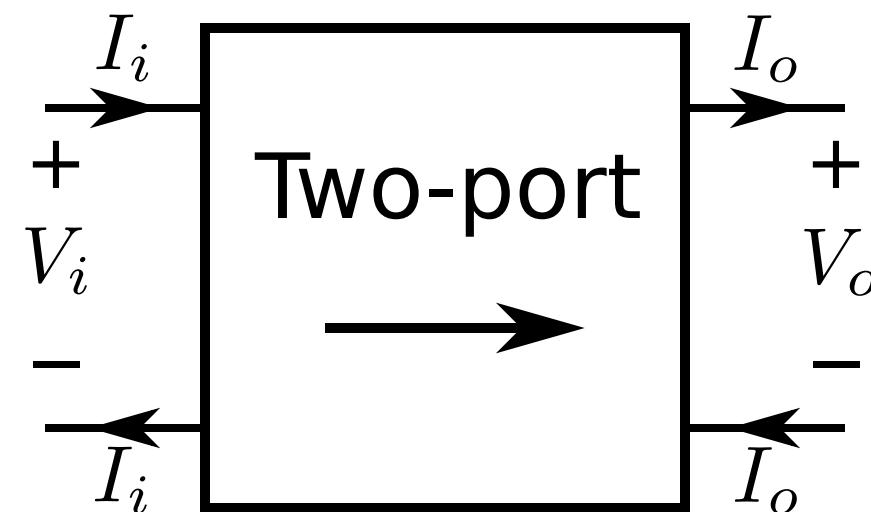
$$A = \frac{1}{\mu} = \left. \frac{V_i}{V_o} \right|_{I_o=0},$$

$$B = \frac{1}{\gamma} = \left. \frac{V_i}{I_o} \right|_{V_o=0},$$

Open output

Shorted output

Two-port modeling: Chapter 18.6

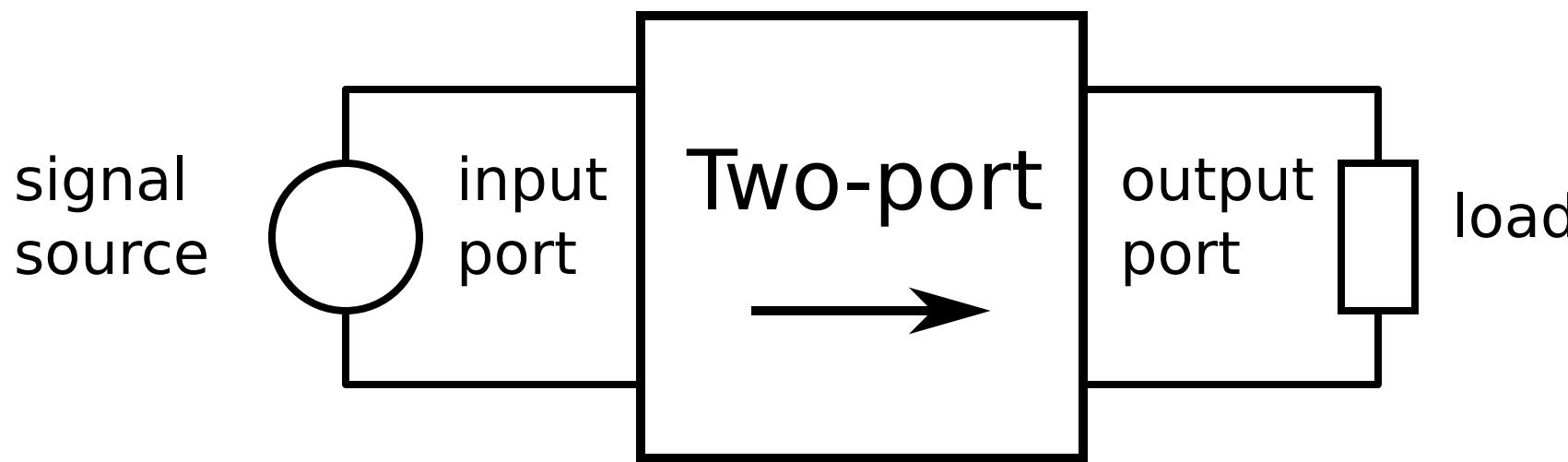


Two-port
conditions

Two-port
representations

Two-port model

Functional model:
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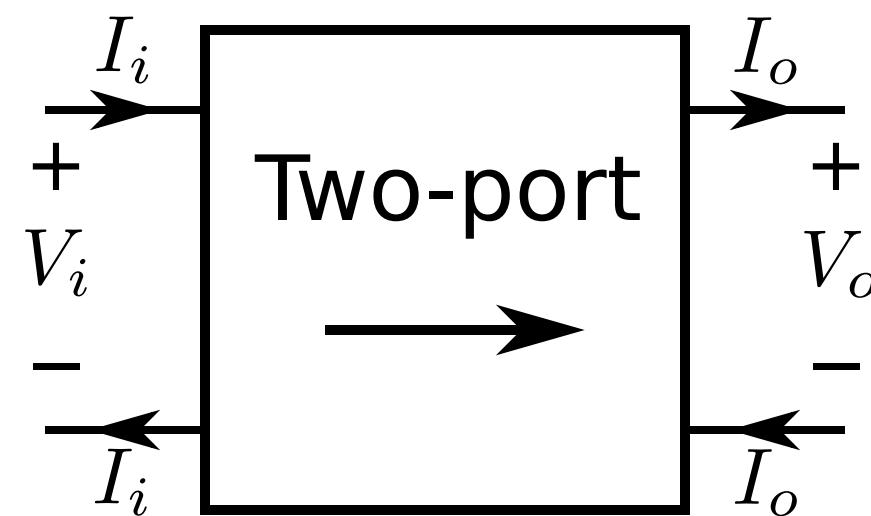
$$C = \frac{1}{\zeta} = \left. \frac{I_i}{V_o} \right|_{I_o=0},$$

Open output

Shorted output

Open output

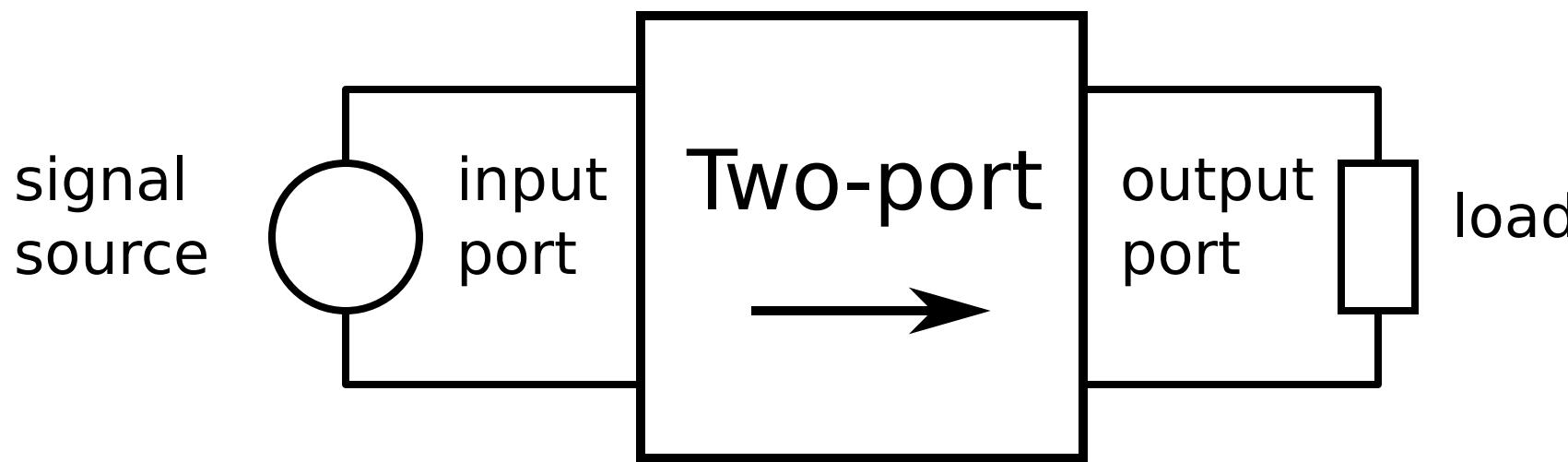
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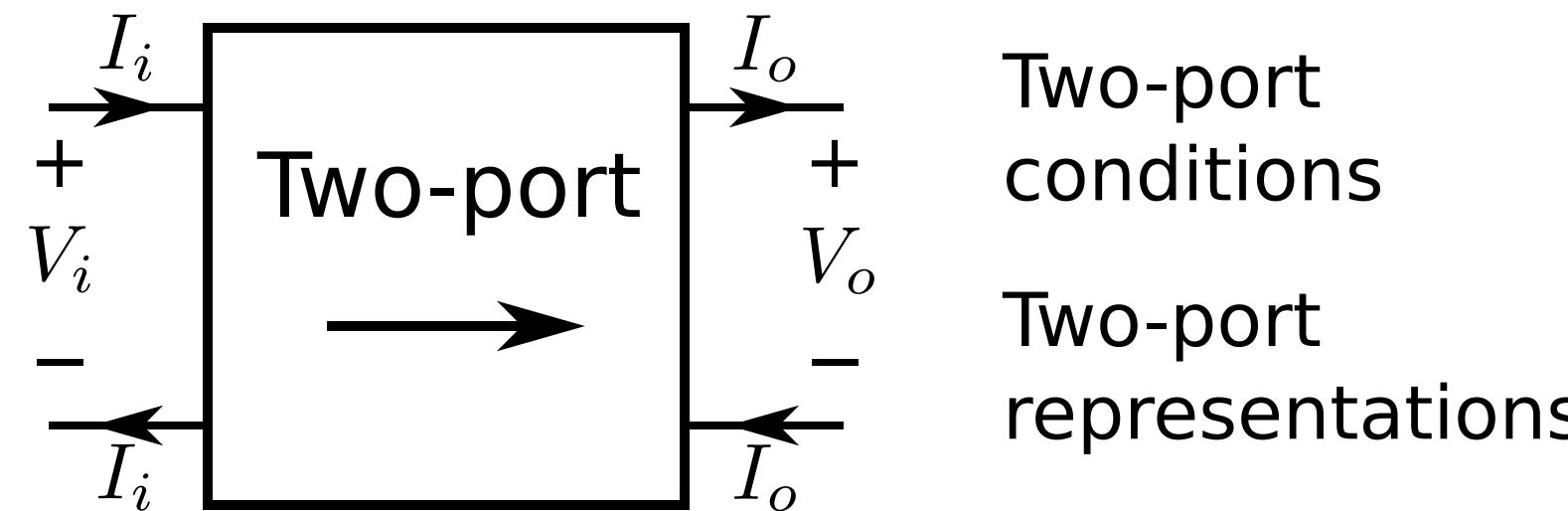
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$$D = \frac{1}{\alpha} = \left. \frac{I_i}{I_o} \right|_{V_o=0}.$$

Open output

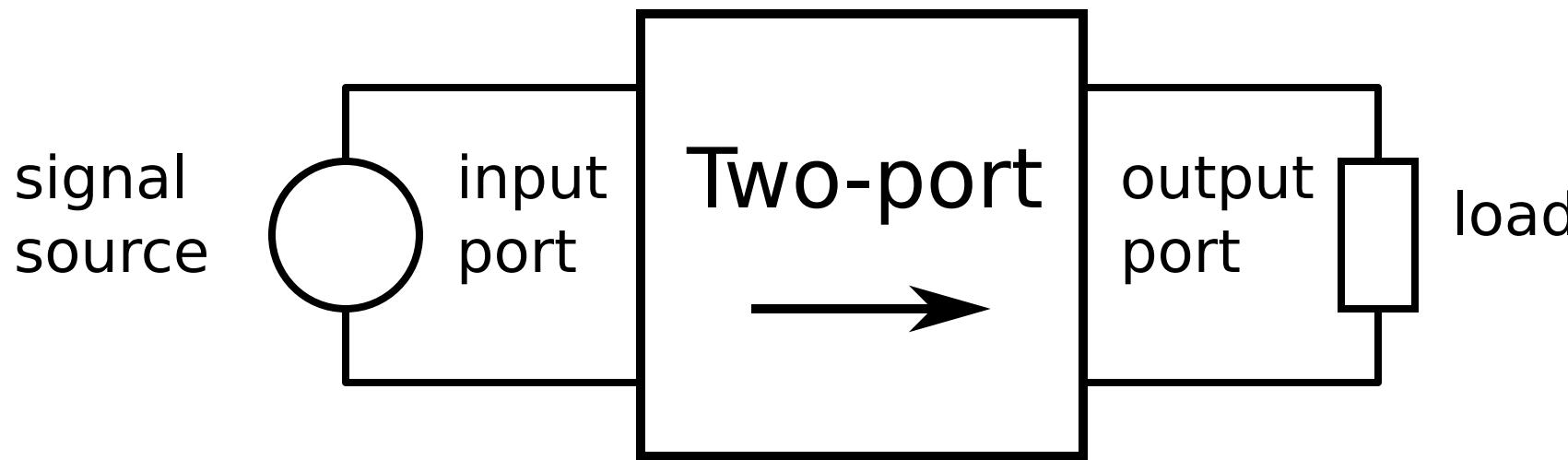
Shorted output

Open output

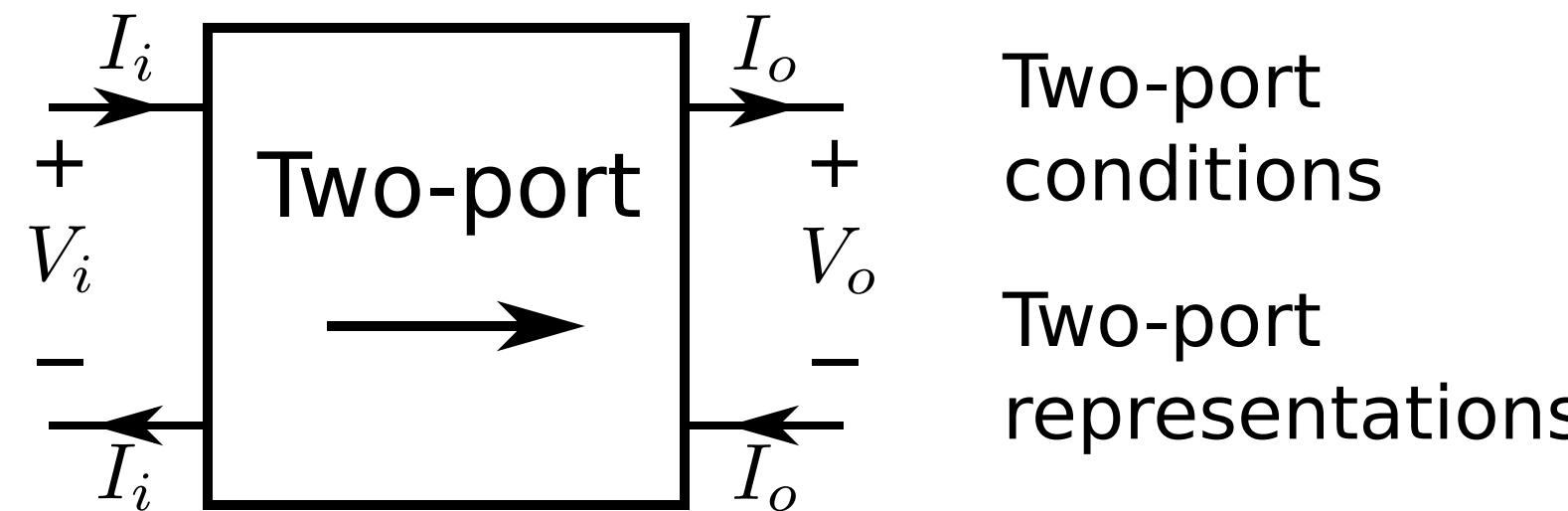
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Open output

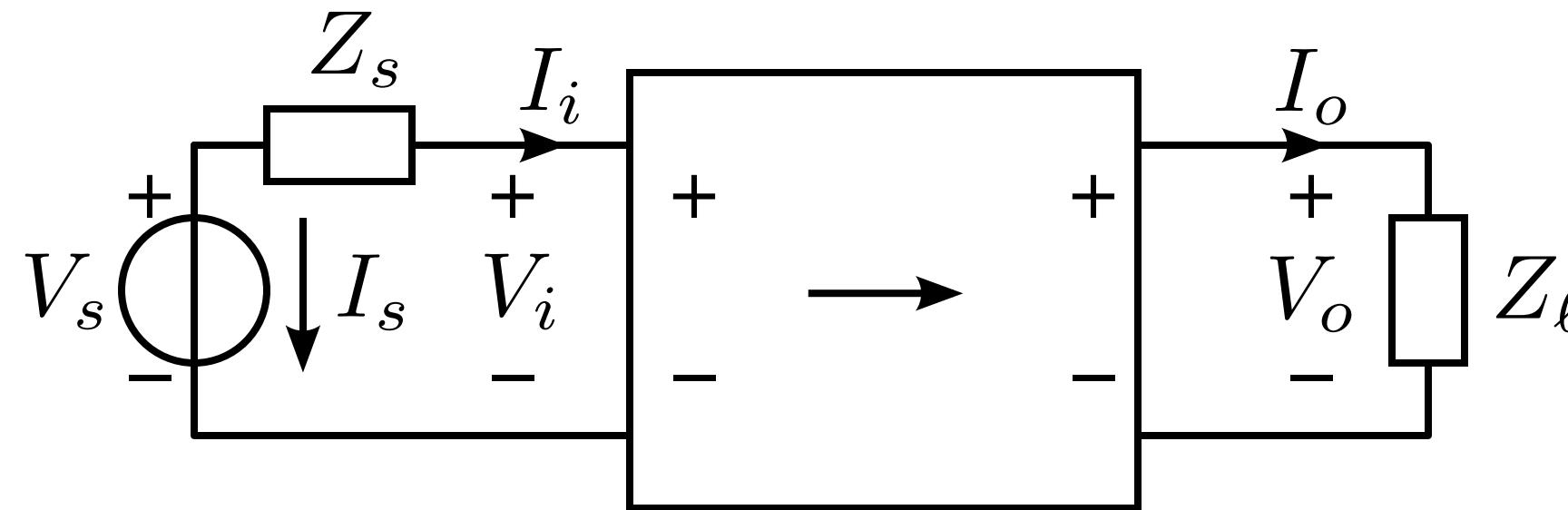
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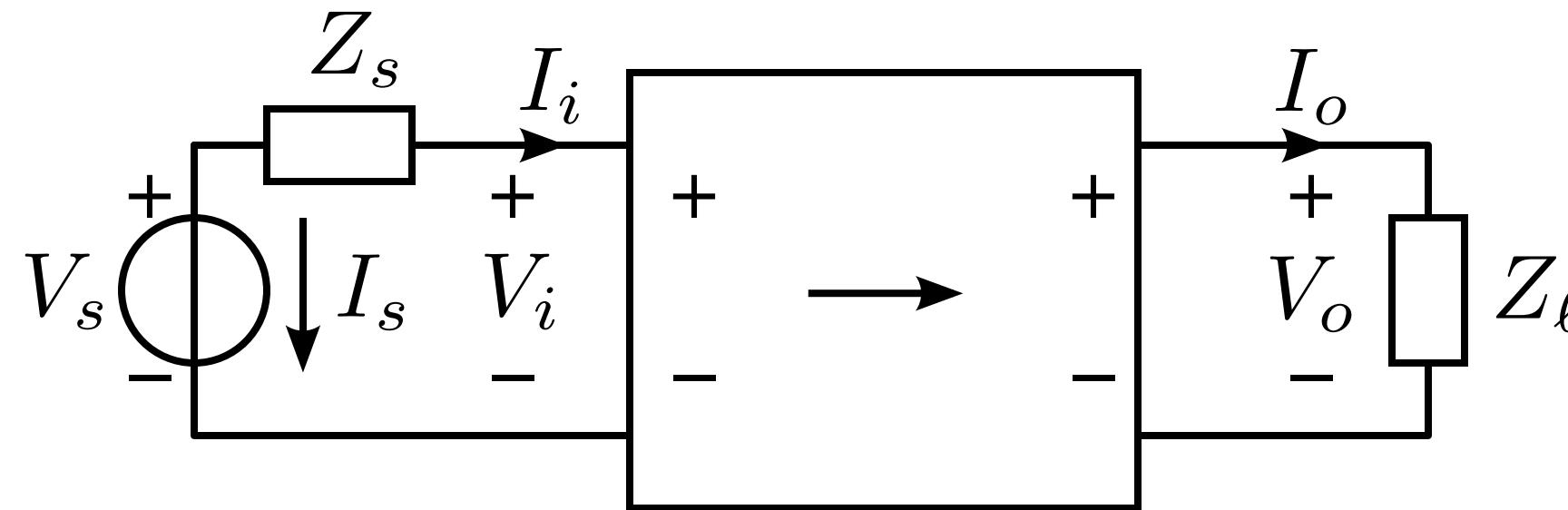
Shorted output

Determination of the transmission-1 two-port parameters

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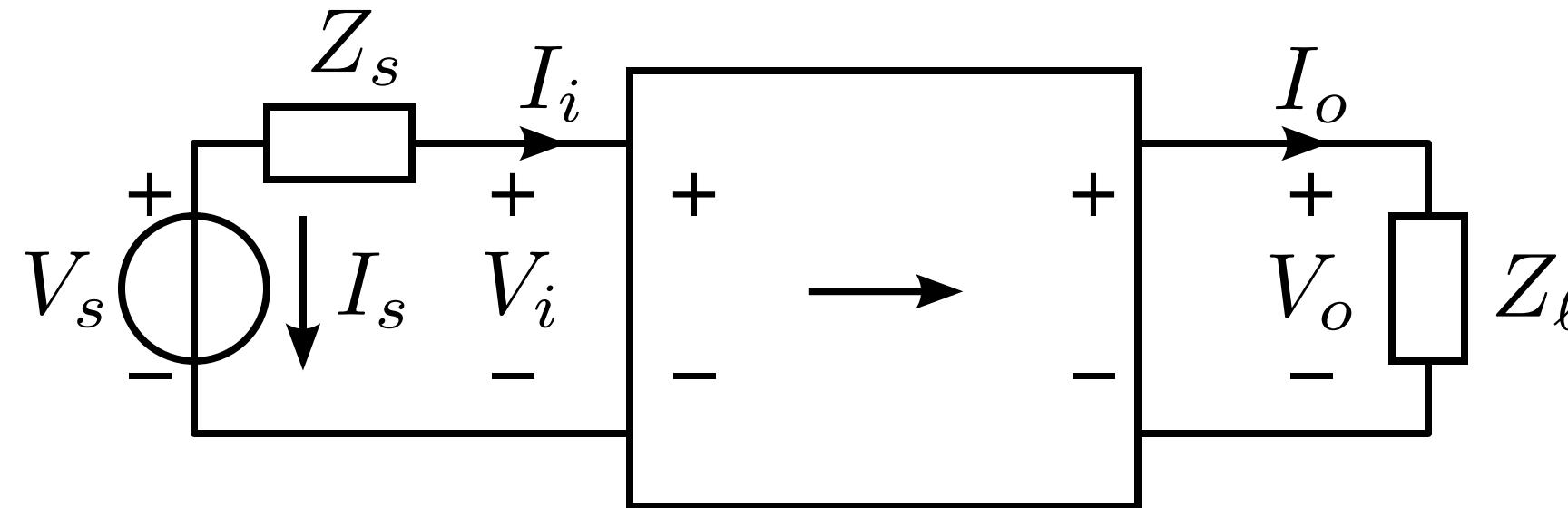


Determination of the transmission-1 two-port parameters



$$\mu = \frac{1}{A} = \left. \frac{V_o}{V_i} \right|_{I_o=0}$$

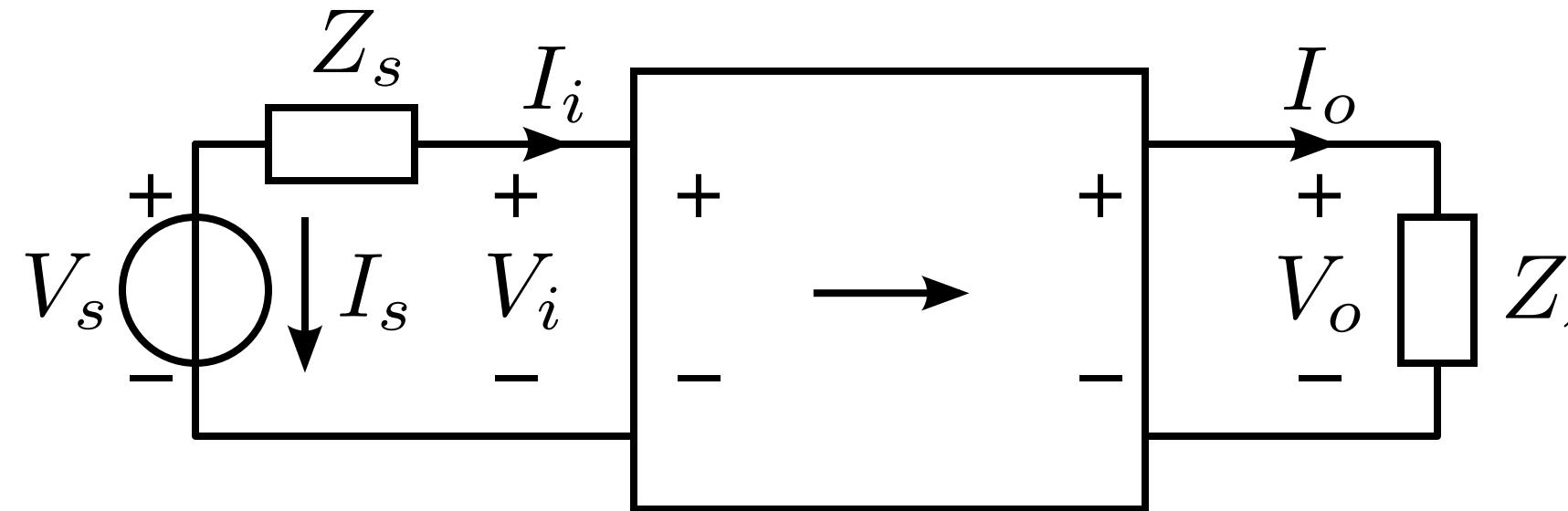
Determination of the transmission-1 two-port parameters



$$\mu = \frac{1}{A} = \left. \frac{V_o}{V_i} \right|_{I_o=0}$$

$$A = \lim_{Z_\ell \rightarrow \infty} \left(\frac{V_i}{V_o} \right)$$

Determination of the transmission-1 two-port parameters



$$\mu = \frac{1}{A} = \left. \frac{V_o}{V_i} \right|_{I_o=0}$$

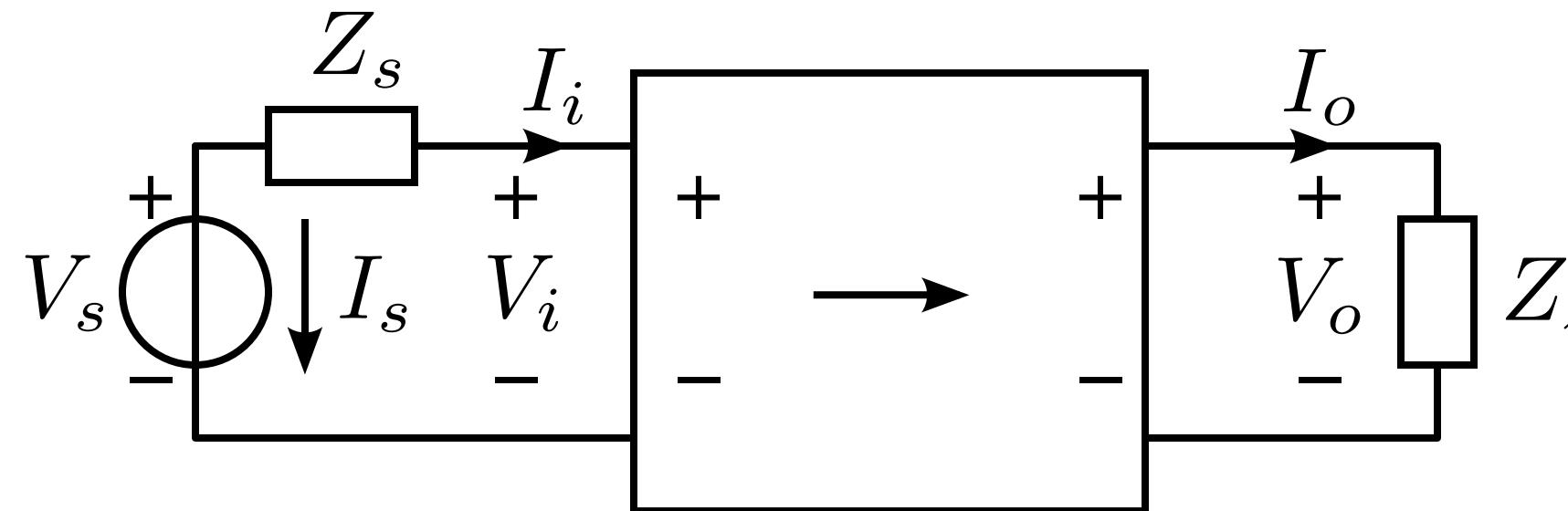
$$A = \lim_{Z_\ell \rightarrow \infty} \left(\frac{V_i}{V_o} \right)$$

$$\zeta = \frac{1}{C} = \left. \frac{V_o}{I_i} \right|_{I_o=0}$$

$$C = \lim_{Z_\ell \rightarrow \infty} \left(\frac{I_i}{V_o} \right)$$

$$\gamma = \frac{1}{B} = \left. \frac{I_o}{V_i} \right|_{V_o=0}$$

Determination of the transmission-1 two-port parameters



$$\mu = \frac{1}{A} = \left. \frac{V_o}{V_i} \right|_{I_o=0}$$

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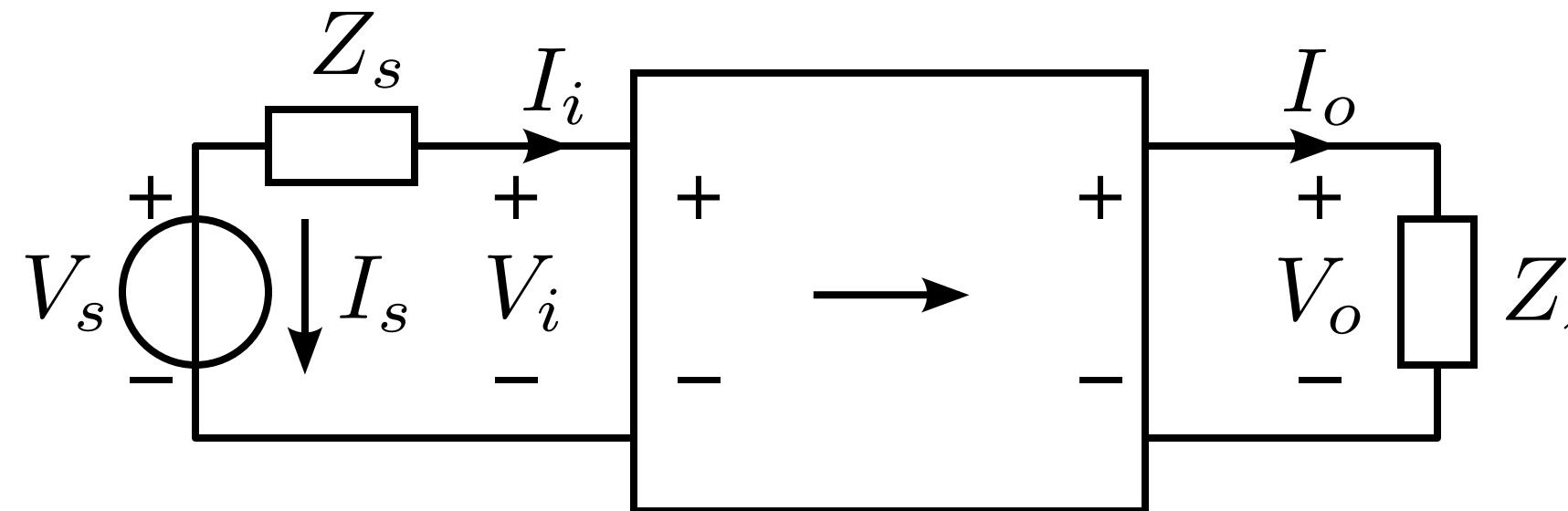
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$$B = \lim_{Z_\ell \rightarrow 0} \left(\frac{V_i}{I_o} \right)$$

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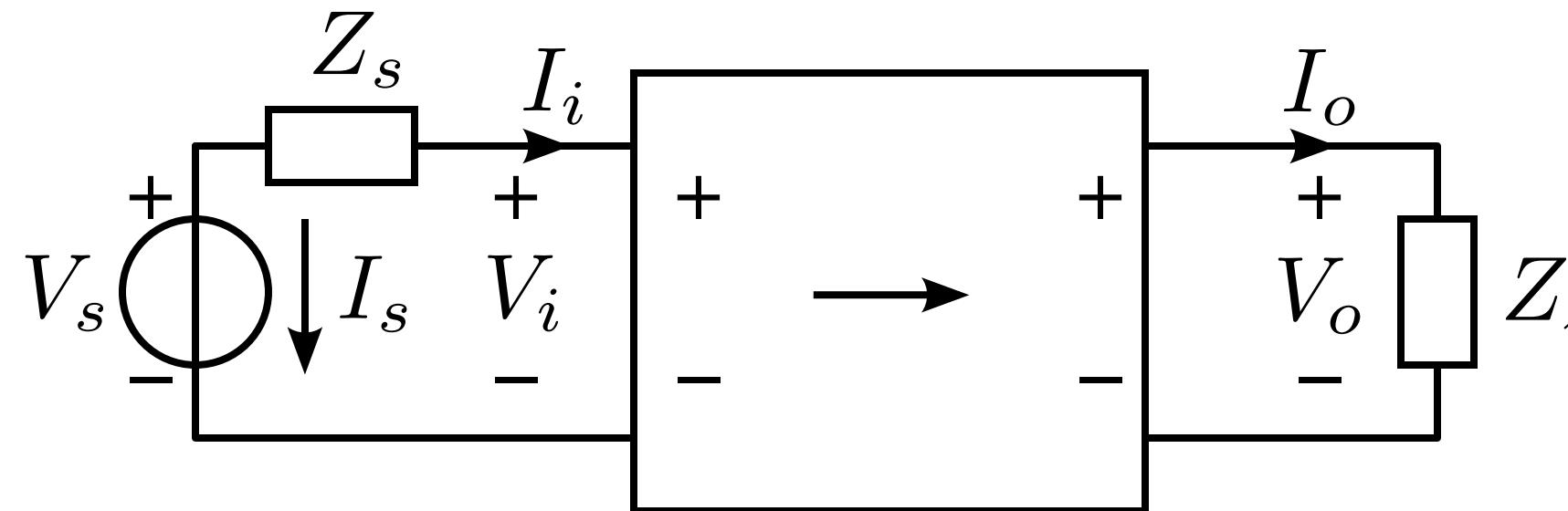
$$C = \lim_{Z_\ell \rightarrow \infty} \left(\frac{I_i}{V_o} \right)$$

$$\gamma = \frac{1}{B} = \left. \frac{I_o}{V_i} \right|_{V_o=0}$$

$$B = \lim_{Z_\ell \rightarrow 0} \left(\frac{V_i}{I_o} \right)$$

$$\alpha = \frac{1}{D} = \left. \frac{I_o}{I_i} \right|_{V_o=0}$$

Determination of the transmission-1 two-port parameters



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$$A = \lim_{Z_\ell \rightarrow \infty} \left(\frac{V_i}{V_o} \right)$$

$$\zeta = \frac{1}{C} = \left. \frac{V_o}{I_i} \right|_{I_o=0}$$

$$C = \lim_{Z_\ell \rightarrow \infty} \left(\frac{I_i}{V_o} \right)$$

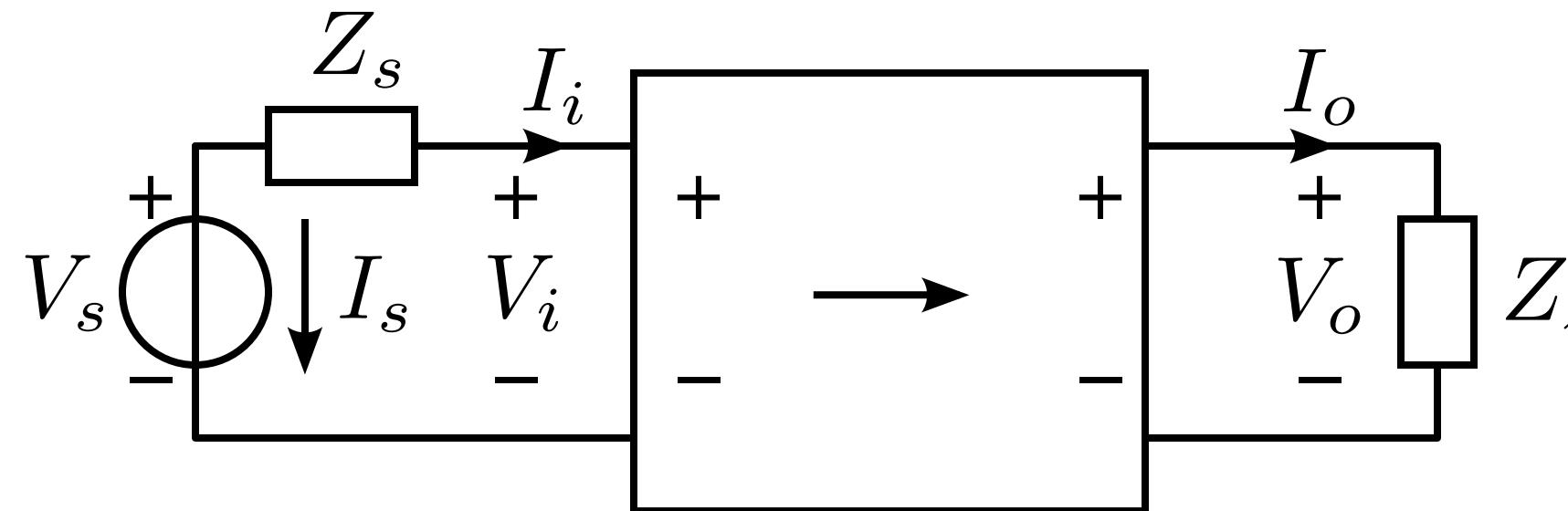
$$\gamma = \frac{1}{B} = \left. \frac{I_o}{V_i} \right|_{V_o=0}$$

$$B = \lim_{Z_\ell \rightarrow 0} \left(\frac{V_i}{I_o} \right)$$

$$\alpha = \frac{1}{D} = \left. \frac{I_o}{I_i} \right|_{V_o=0}$$

$$D = \lim_{Z_\ell \rightarrow 0} \left(\frac{I_i}{I_o} \right)$$

Determination of the transmission-1 two-port parameters



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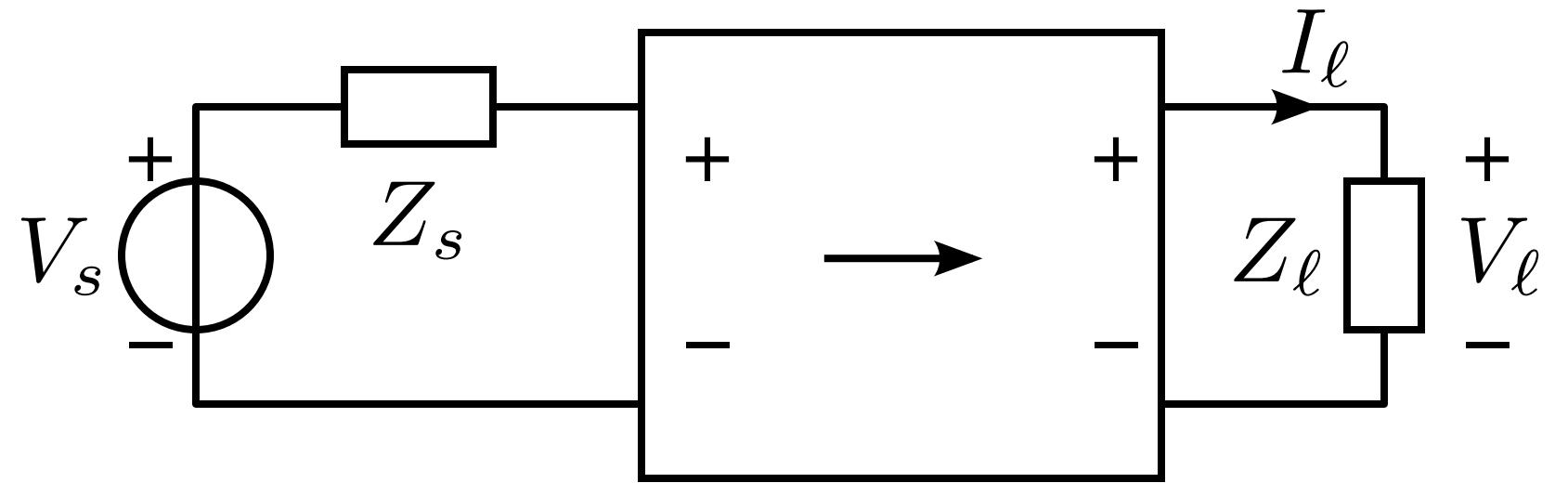
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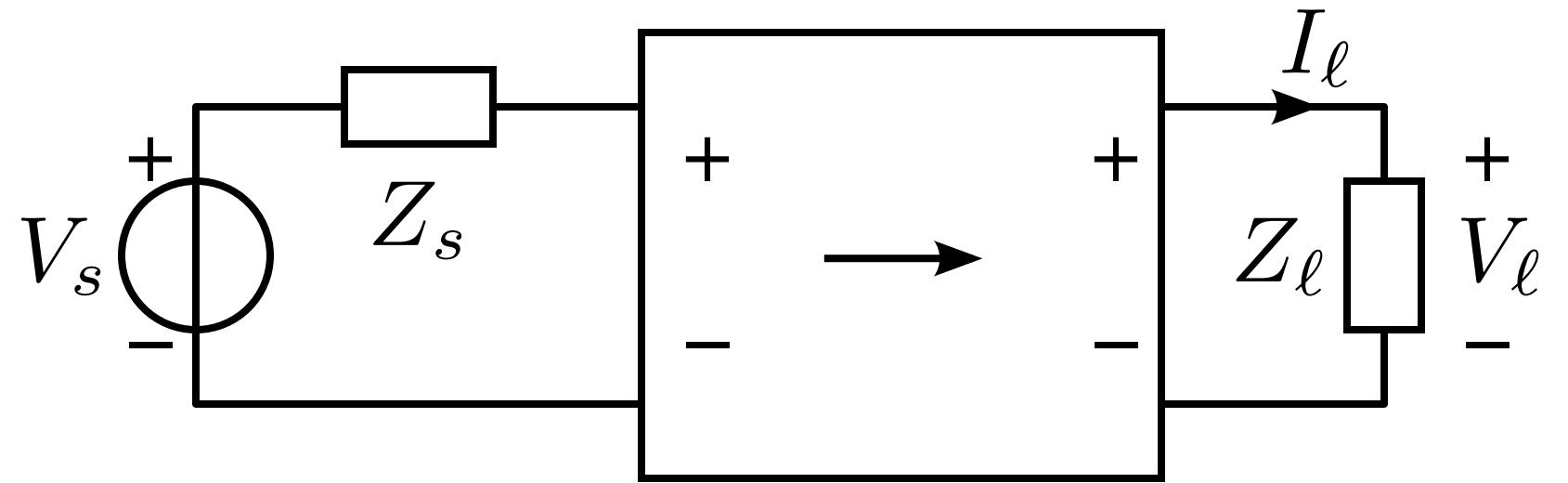
Source to load transfer

Source to load transfer



$$A_v = \frac{V_\ell}{V_s} = \frac{1}{A + B \frac{1}{Z_\ell} + C Z_s + D \frac{Z_s}{Z_\ell}}$$

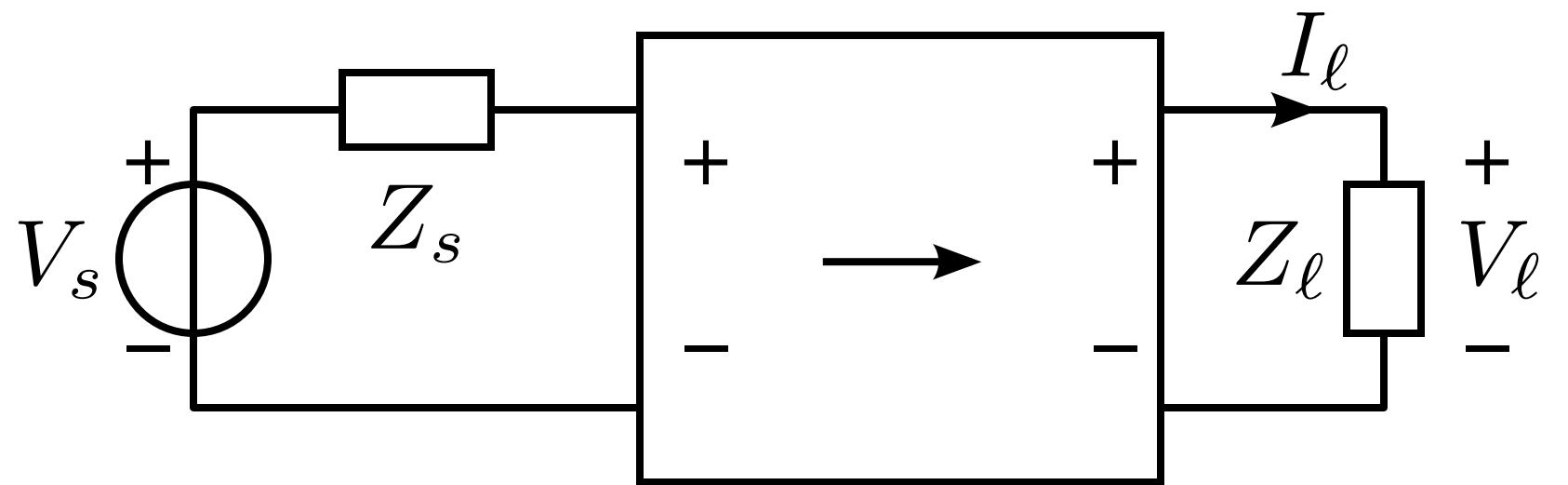
Source to load transfer



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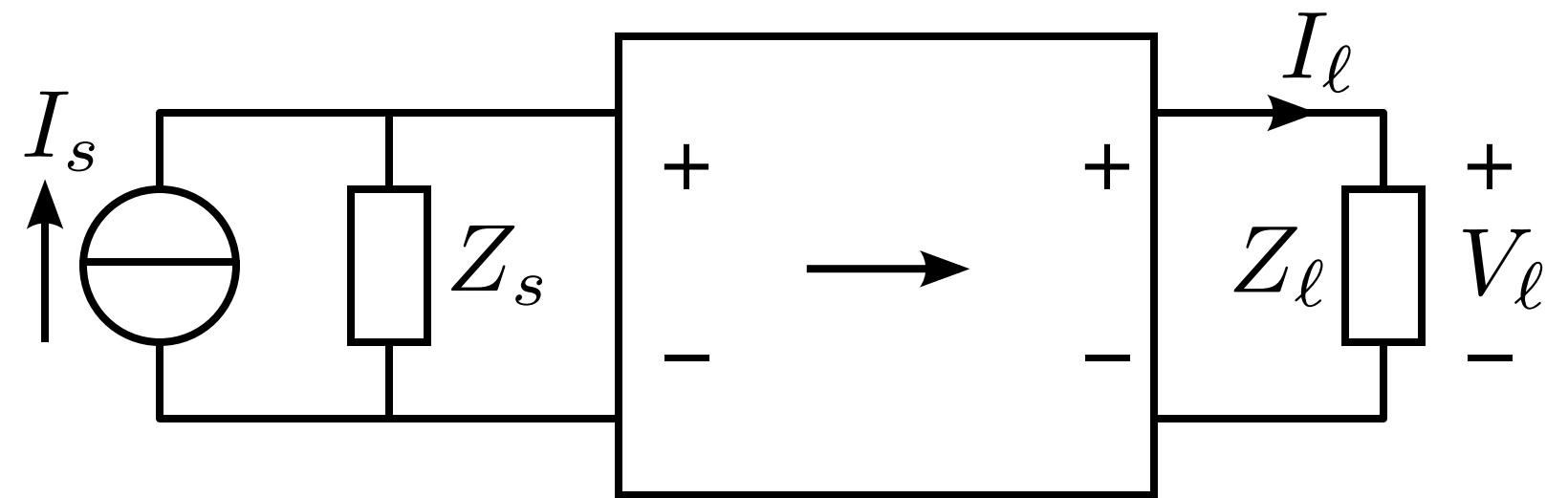
$$A_y = \frac{I_\ell}{V_s} = \frac{1}{A Z_\ell + B + C Z_\ell Z_s + D Z_s}$$

Source to load transfer



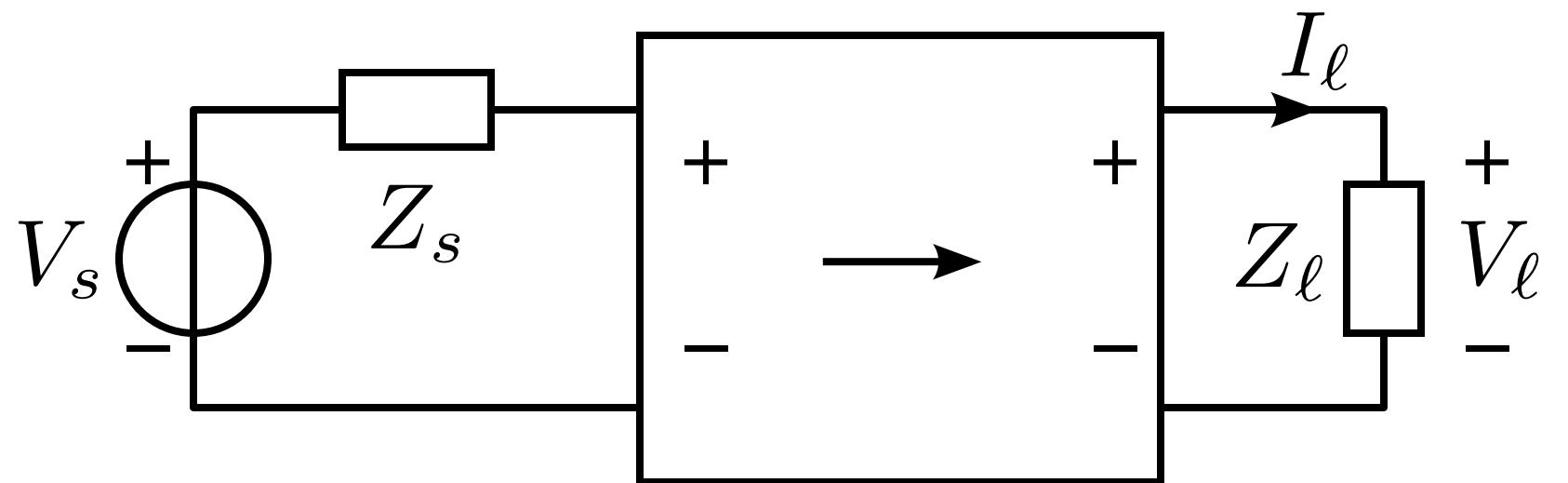
$$A_v = \frac{V_\ell}{V_s} = \frac{1}{A + B \frac{1}{Z_\ell} + C Z_s + D \frac{Z_s}{Z_\ell}}$$

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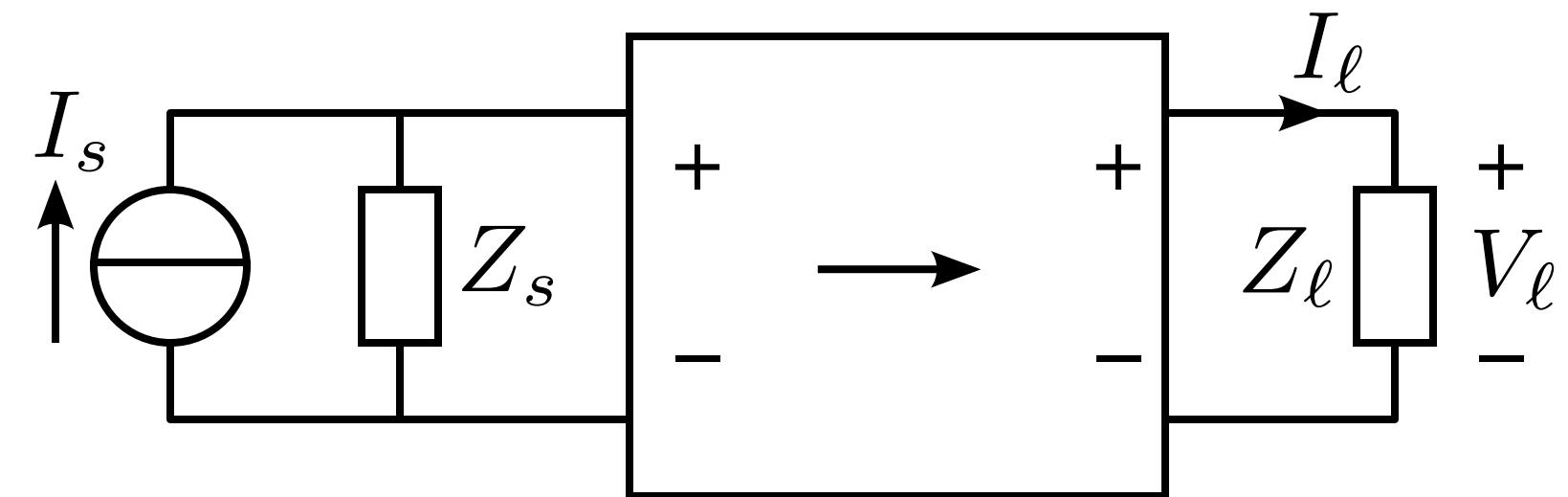
$$A_z = \frac{V_\ell}{I_s} = \frac{1}{A \frac{1}{Z_s} + B \frac{1}{Z_s Z_\ell} + C + D \frac{1}{Z_\ell}}$$

Source to load transfer



$$A_v = \frac{V_\ell}{V_s} = \frac{1}{A + B \frac{1}{Z_\ell} + C Z_s + D \frac{Z_s}{Z_\ell}}$$

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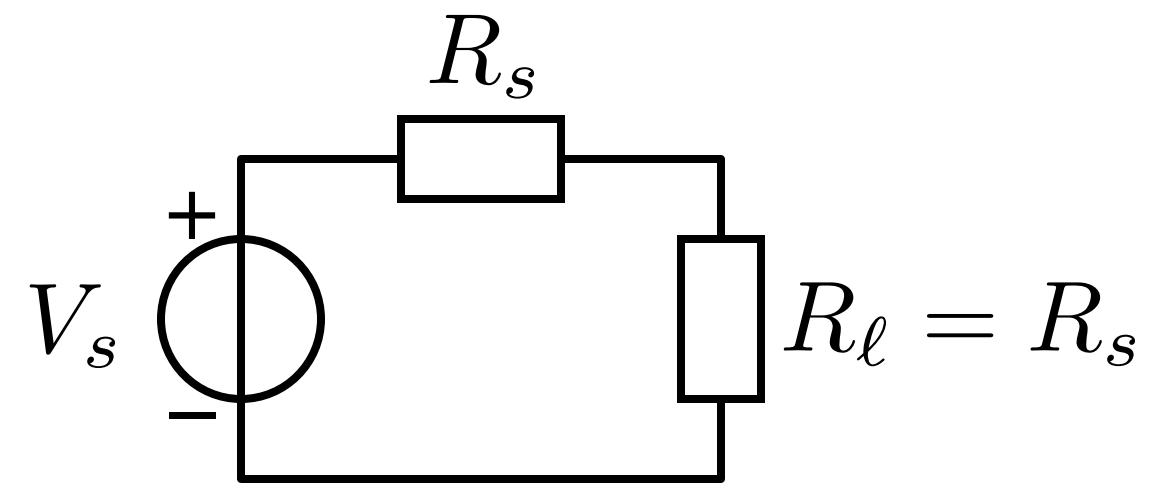


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$$A_i = \frac{I_\ell}{I_s} = \frac{1}{A \frac{Z_\ell}{Z_s} + B \frac{1}{Z_s} + C Z_\ell + D}$$

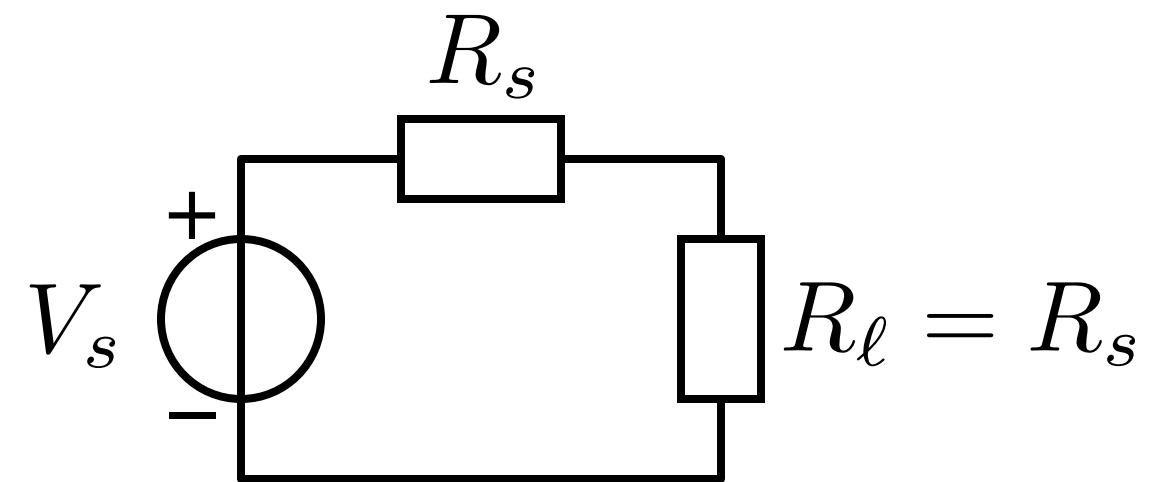
Available power gain

Available power gain



Available power of the source

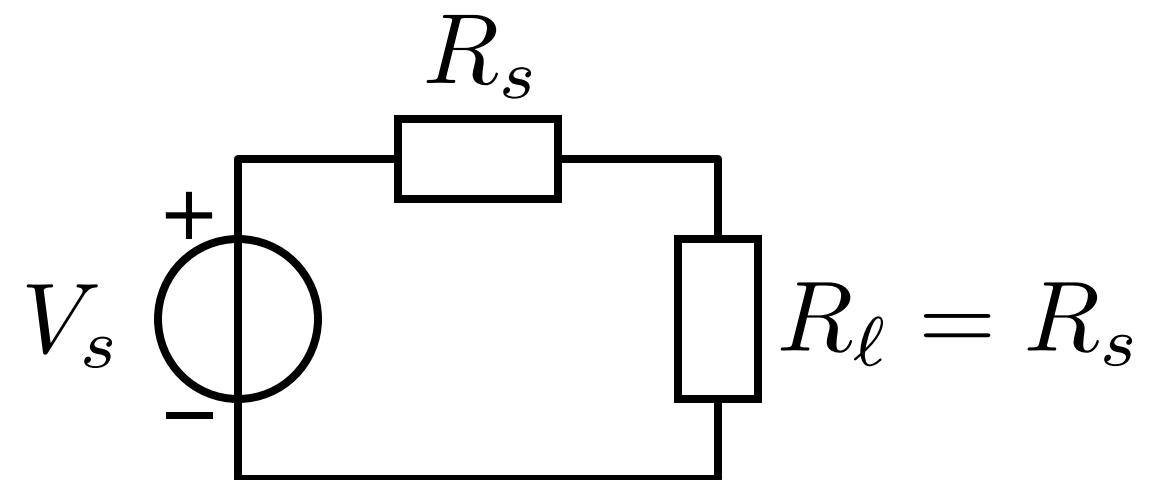
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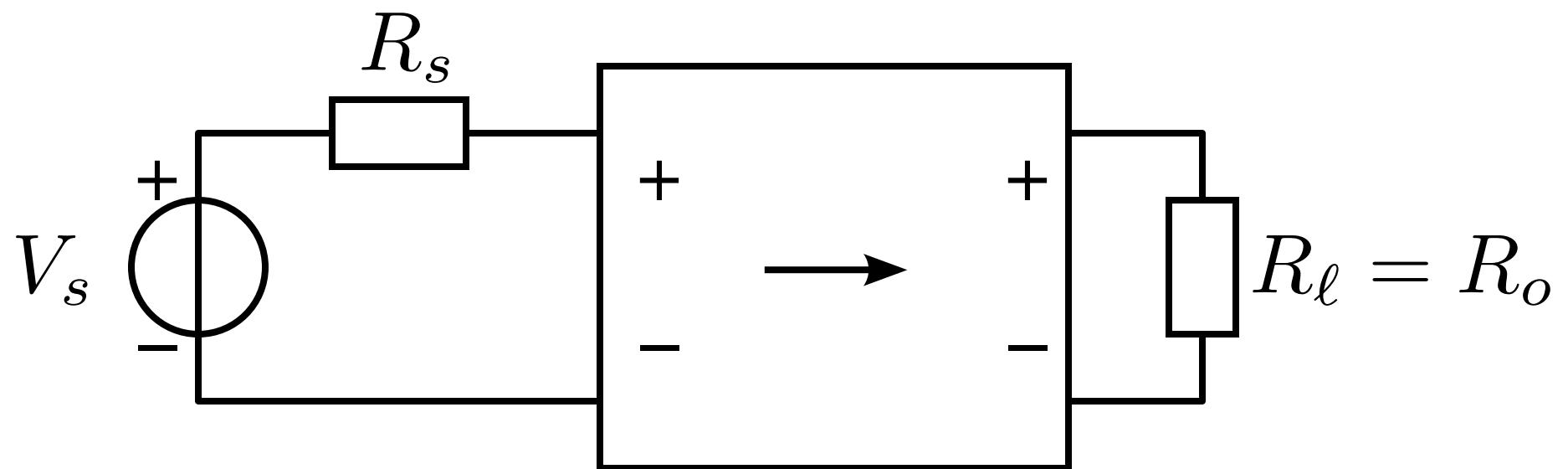
$$P_s = \frac{V_s^2}{4R_s}$$

Available power gain



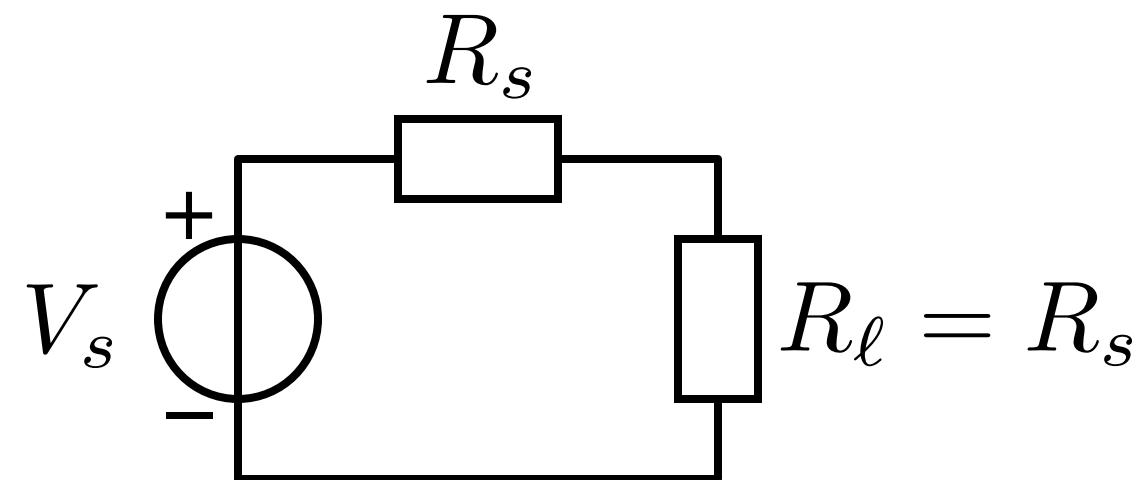
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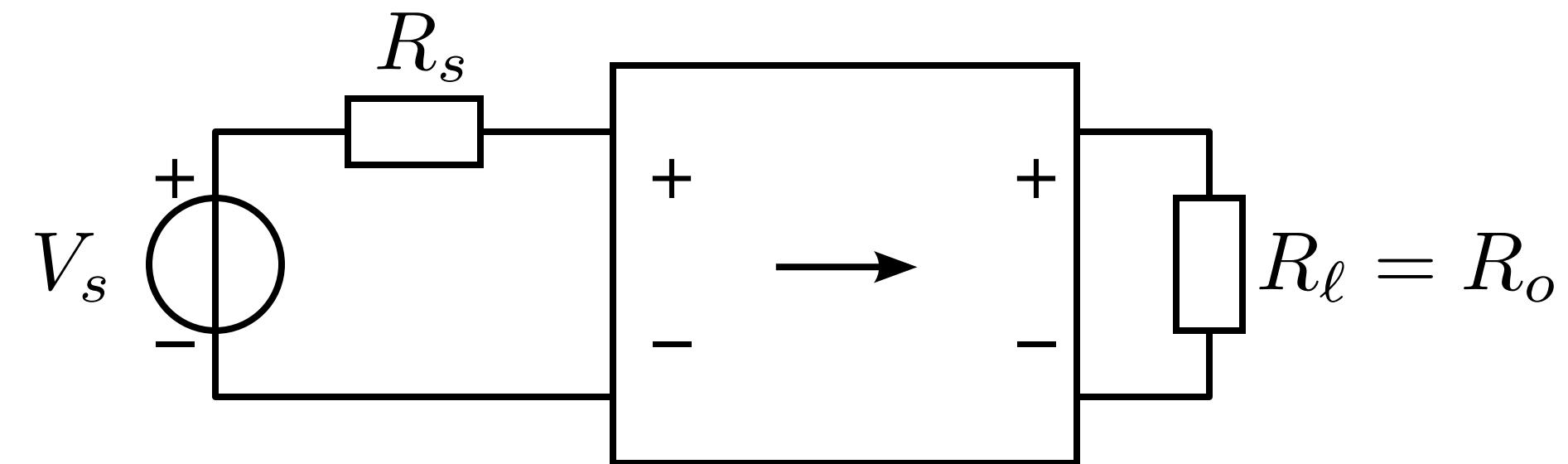
Available power of the amplifier
connected to the source

Available power gain



Available power of the source

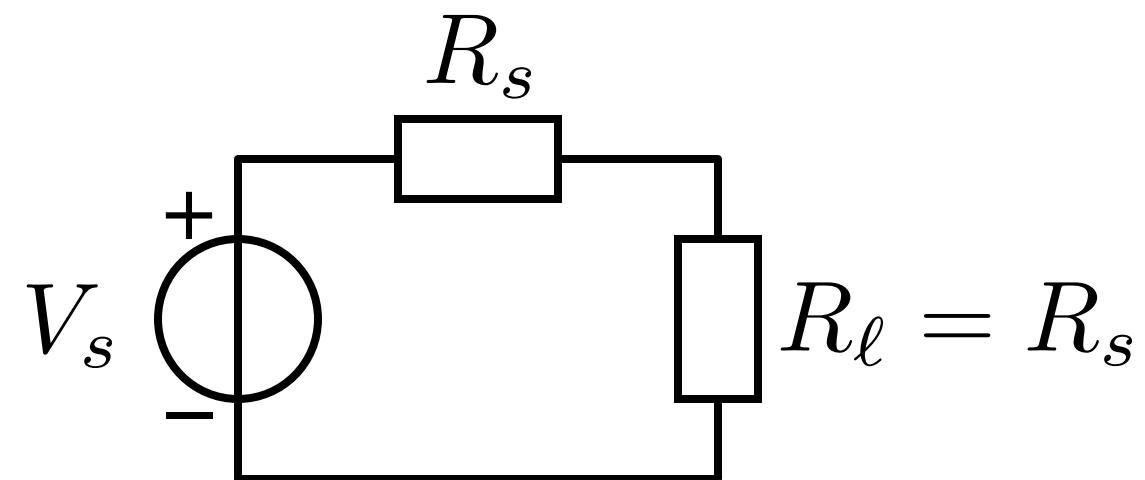
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Available power of the amplifier connected to the source

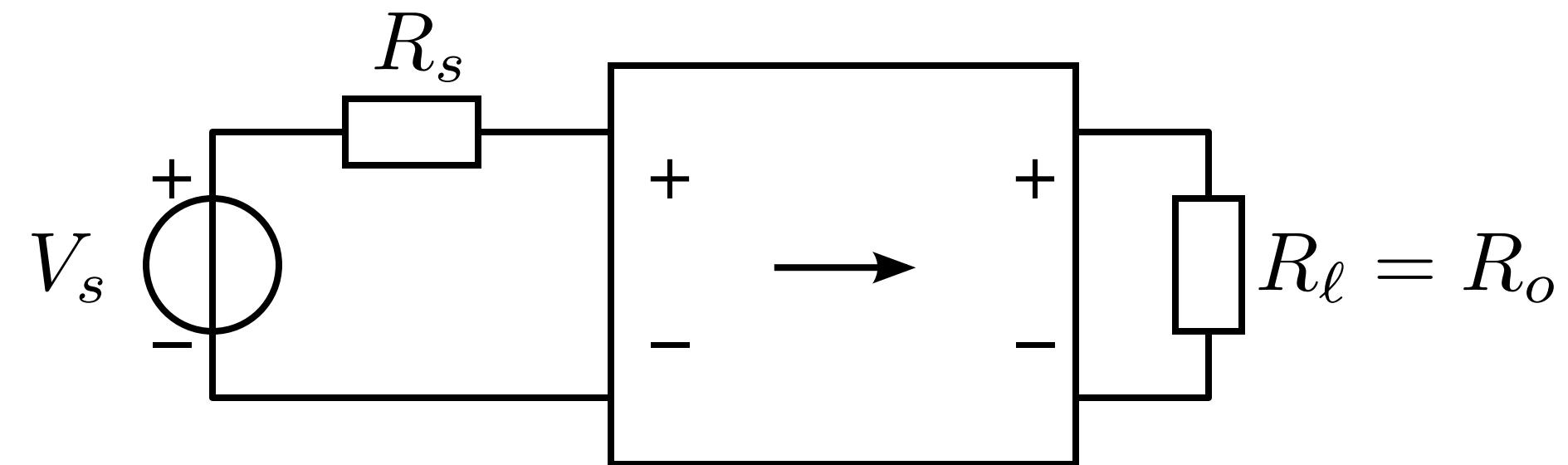
$$P_a = \frac{V_s^2}{4(DR_s + B)(CR_s + A)}$$

Available power gain



Available power of the source

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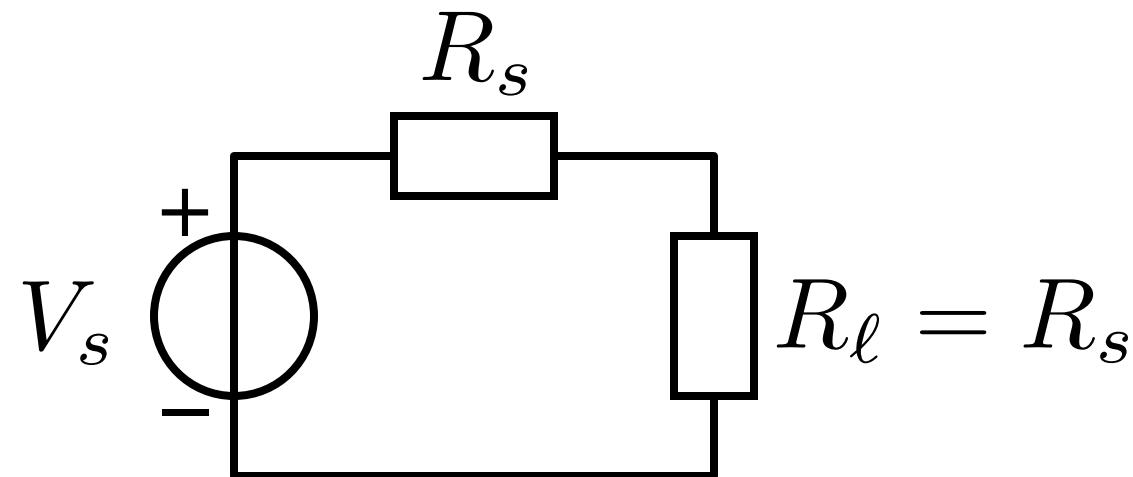


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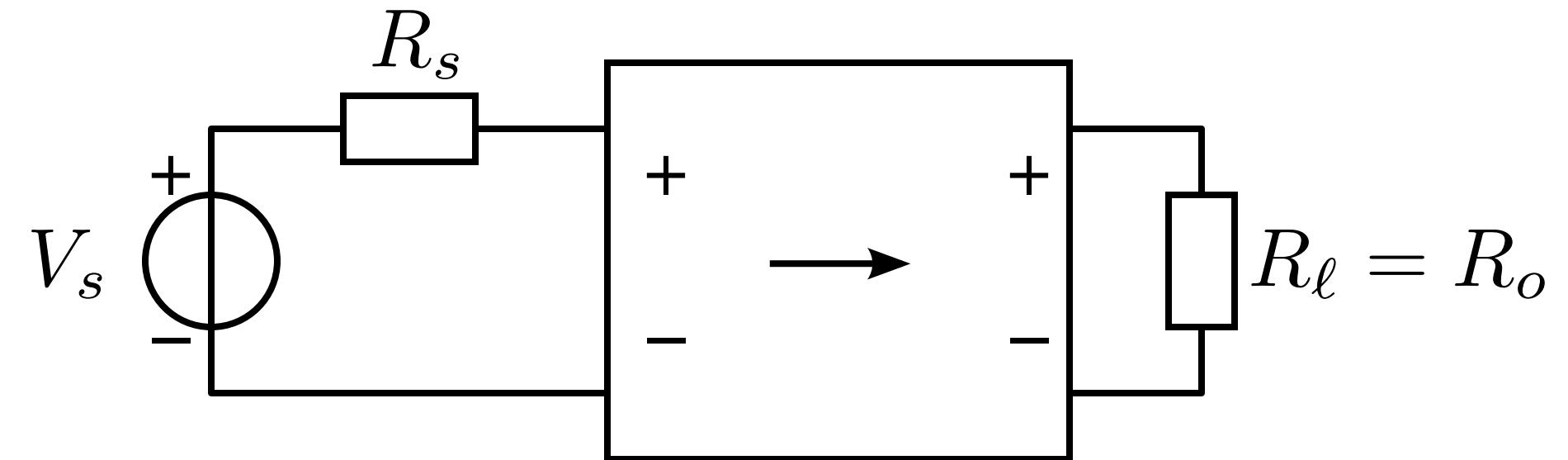
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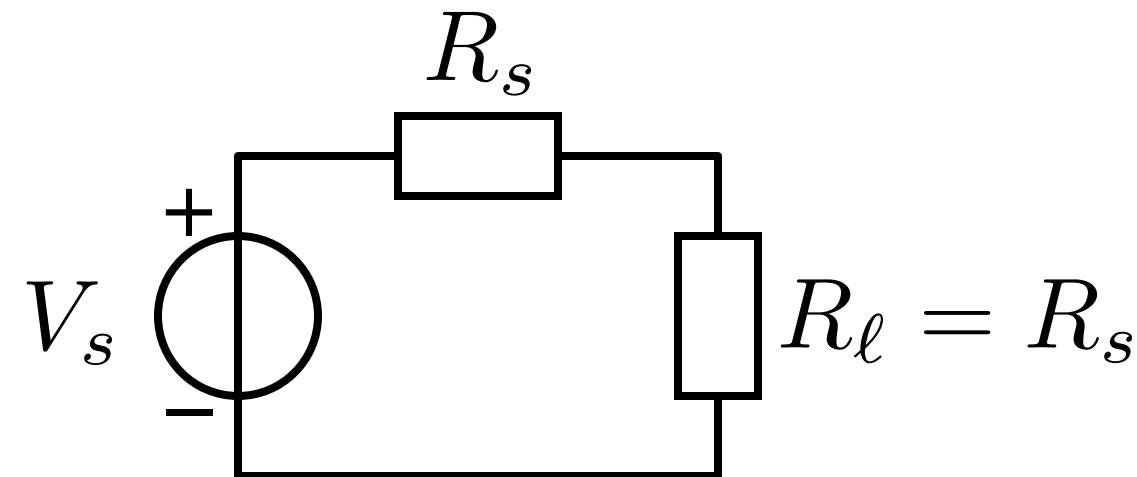
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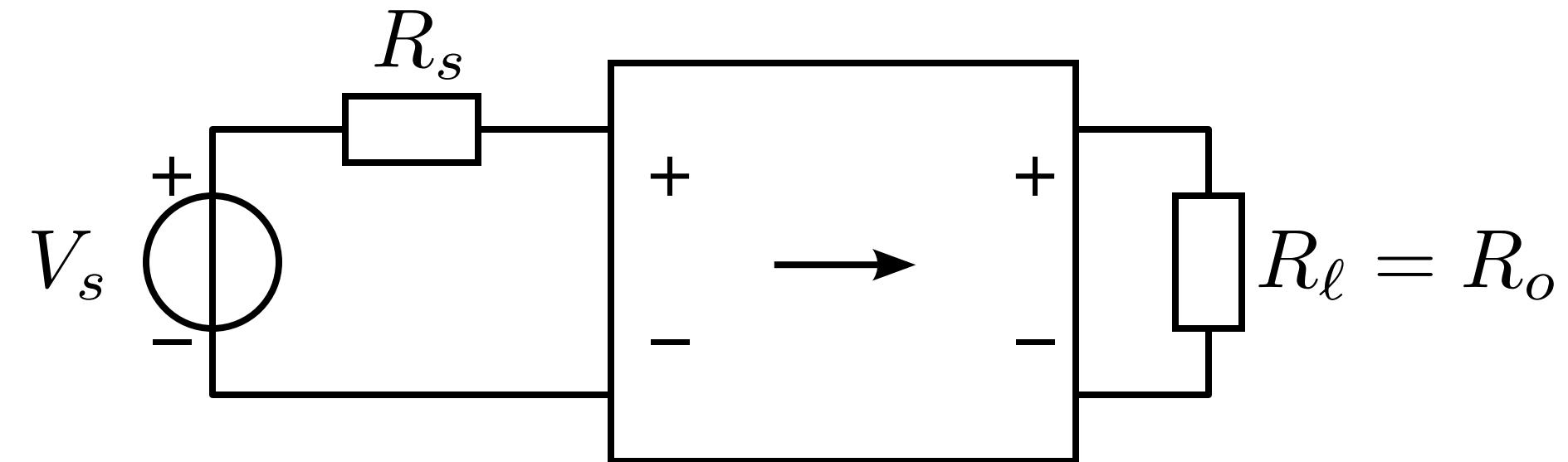
$$G_p = \frac{P_a}{P_s} = \frac{1}{AD + AB/R_s + BC + CD R_s}$$

Available power gain



Available power of the source

$$P_s = \frac{V_s^2}{4R_s}$$



Available power of the amplifier
connected to the source

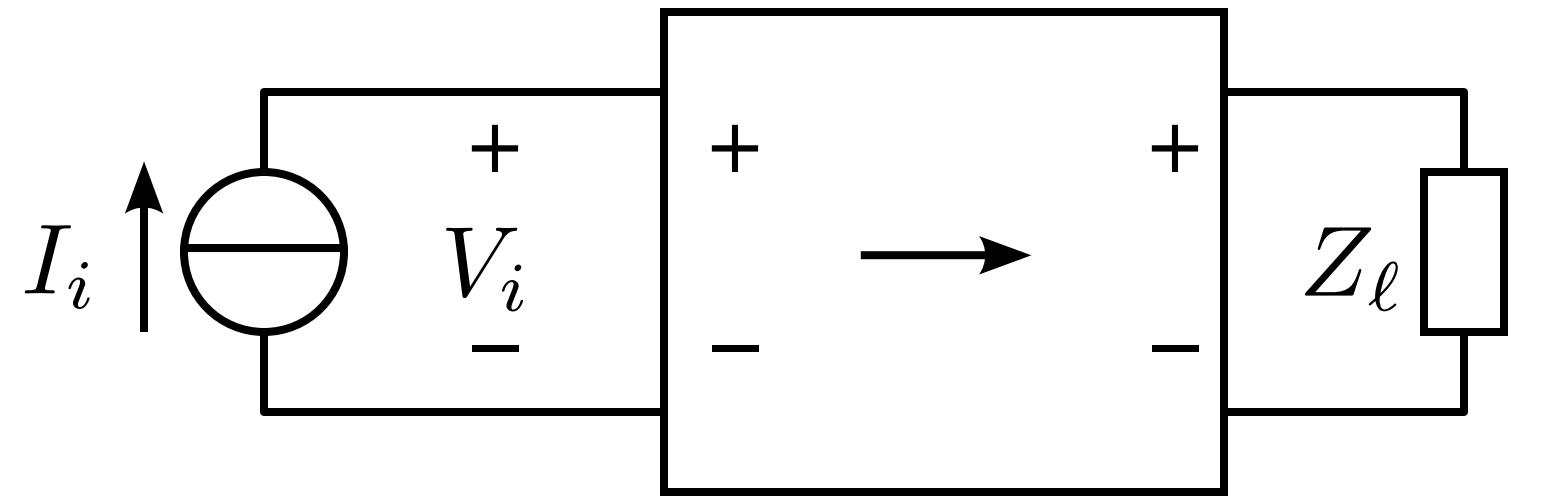
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Available power gain

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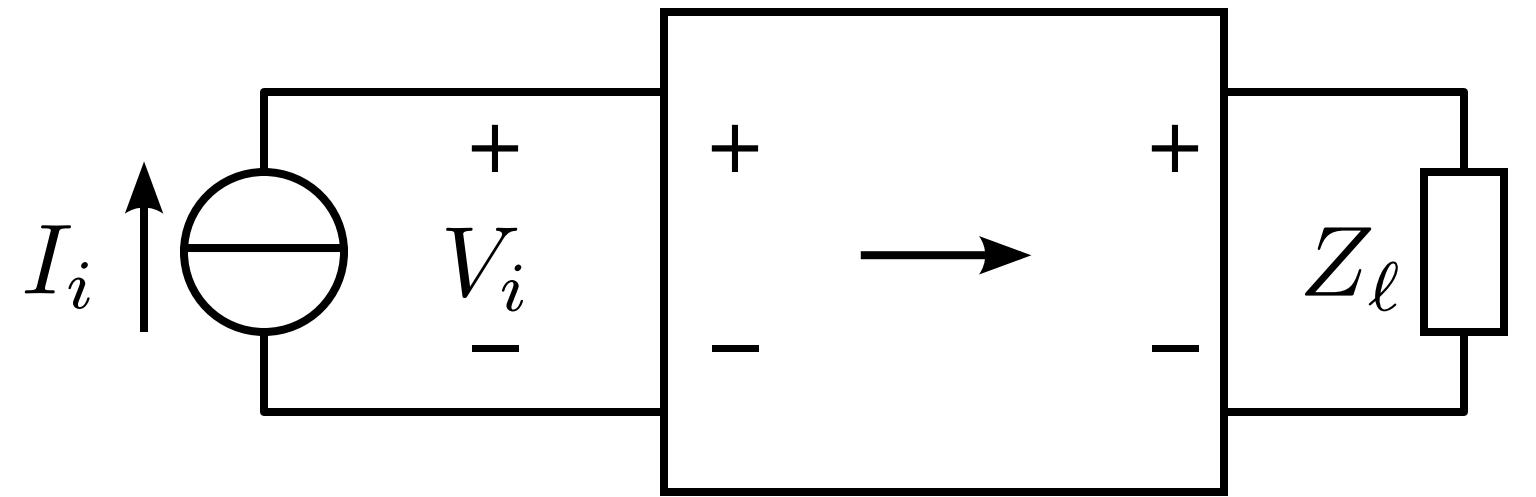
Port impedances

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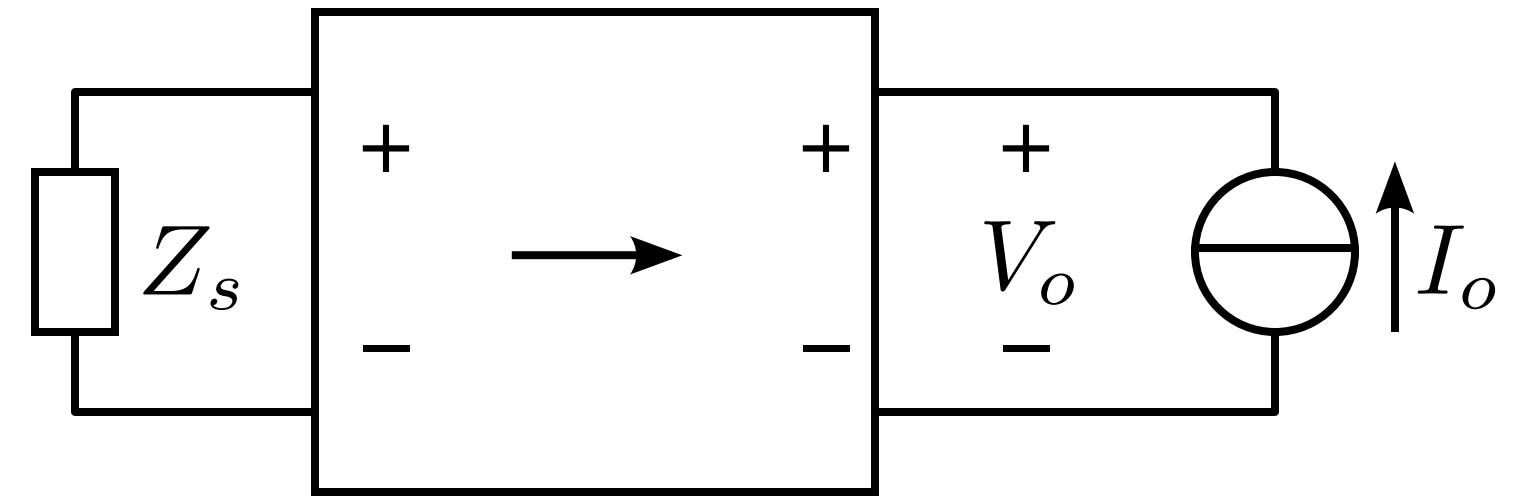


$$Z_i = \frac{V_i}{I_i} = \frac{AZ_\ell + B}{CZ_\ell + D}$$

Port impedances

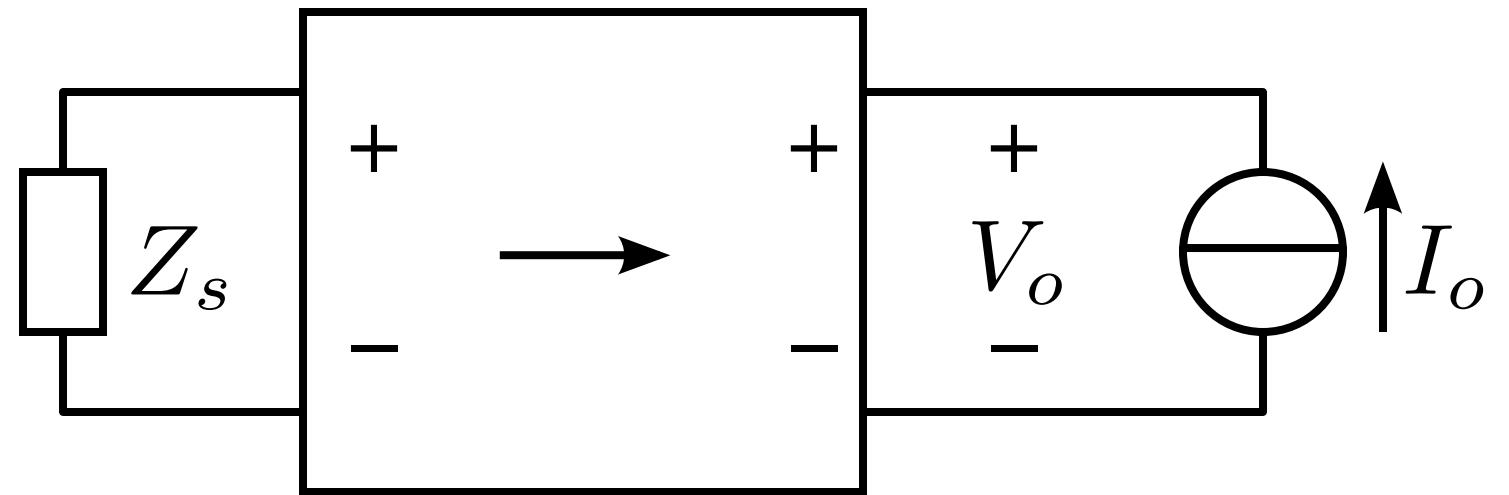
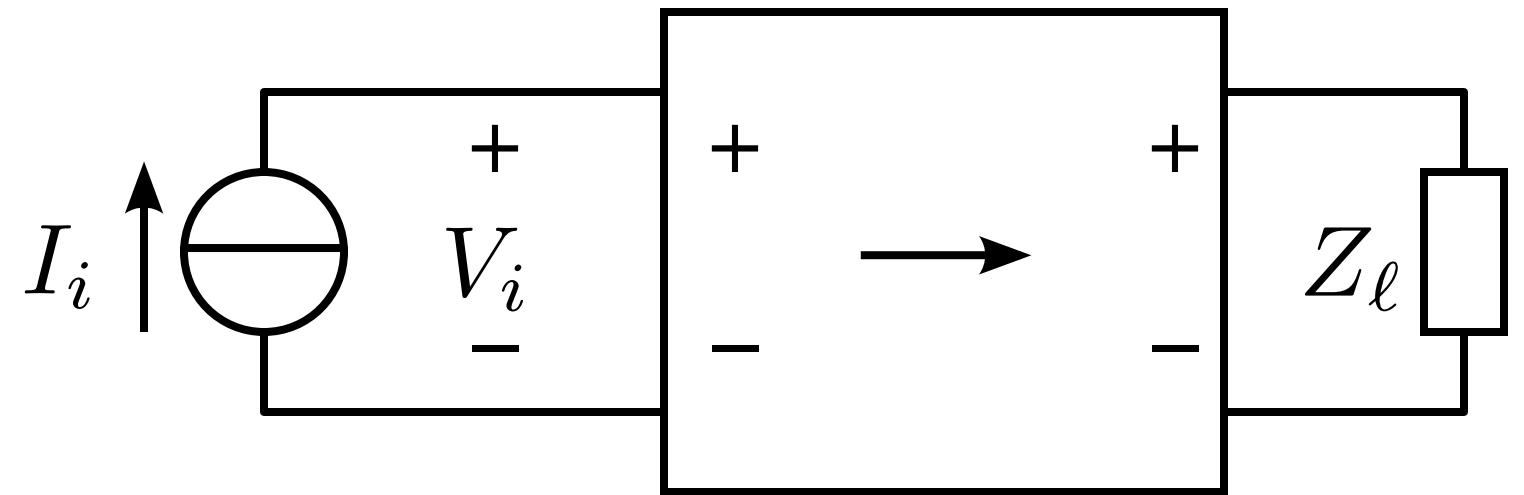


$$Z_i = \frac{V_i}{I_i} = \frac{AZ_\ell + B}{CZ_\ell + D}$$



$$Z_o = \frac{V_o}{I_o} = \frac{DZ_s + B}{CZ_s + A}$$

Port impedances



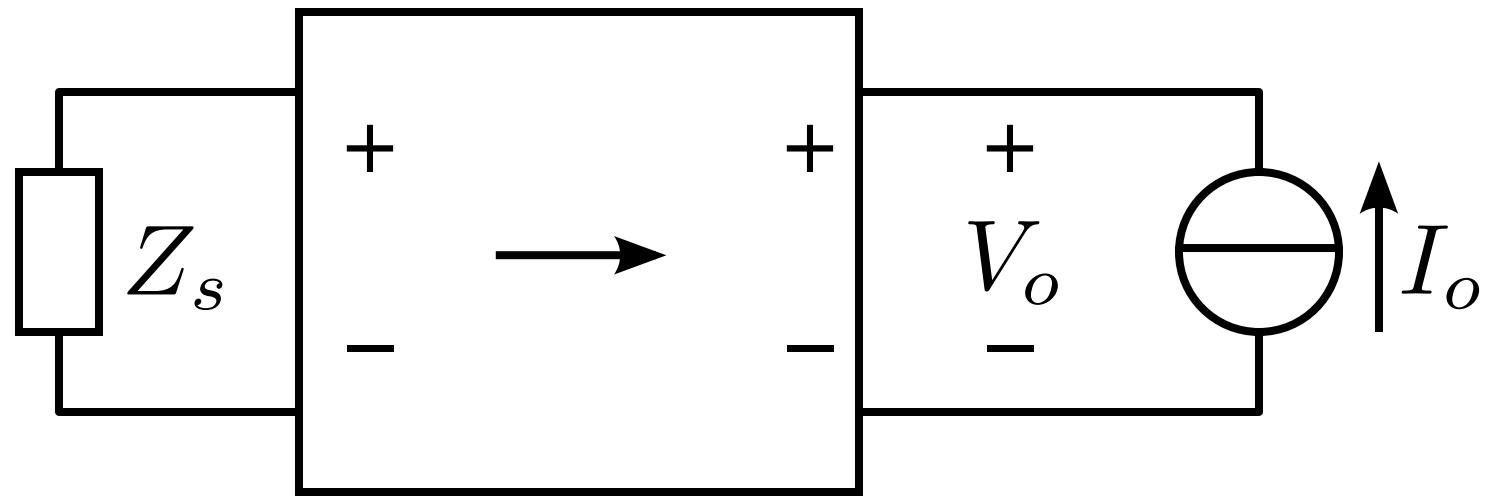
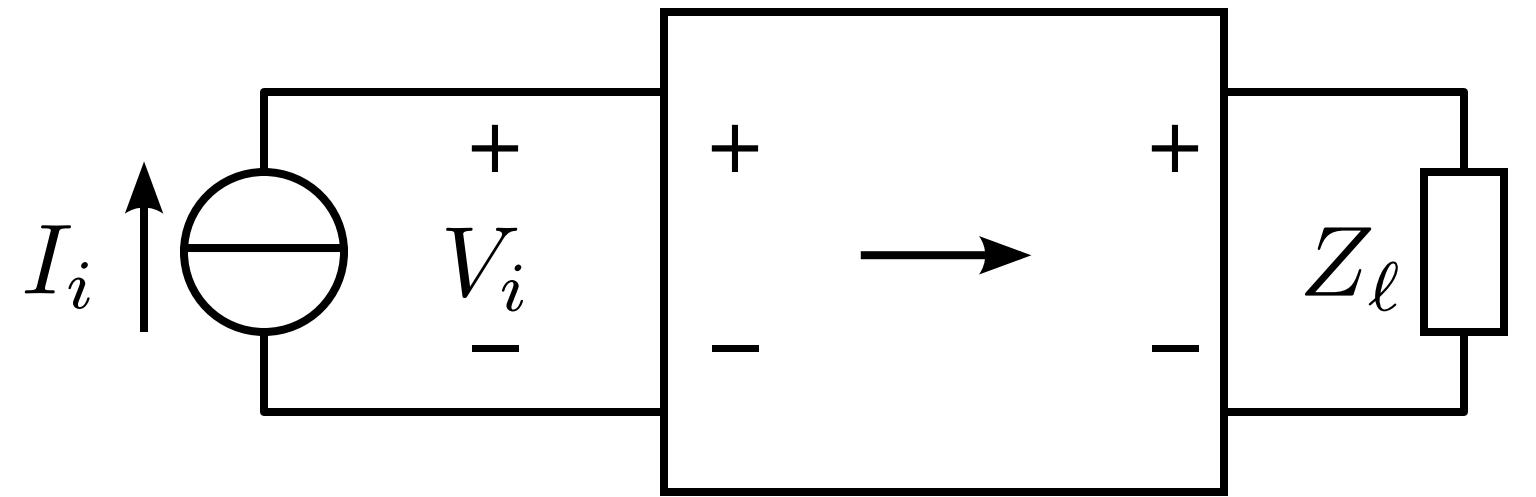
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$$Z_o = \frac{V_o}{I_o} = \frac{DZ_s + B}{CZ_s + A}$$

Unilateral if:

$$AD = BC$$

Port impedances



$$Z_i = \frac{V_i}{I_i} = \frac{AZ_\ell + B}{CZ_\ell + D}$$

$$Z_o = \frac{V_o}{I_o} = \frac{DZ_s + B}{CZ_s + A}$$

Unilateral if:

$$AD = BC$$

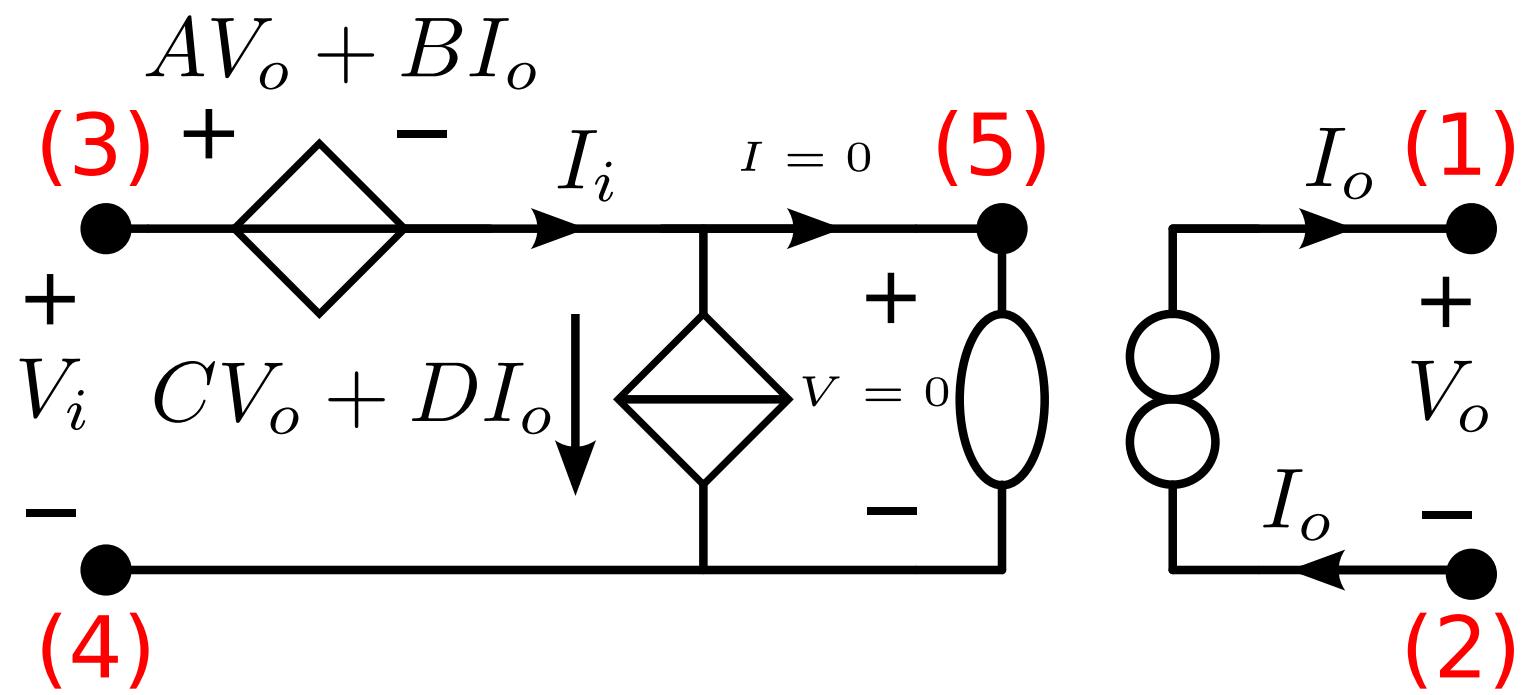
Amplifier types

Amplifier types

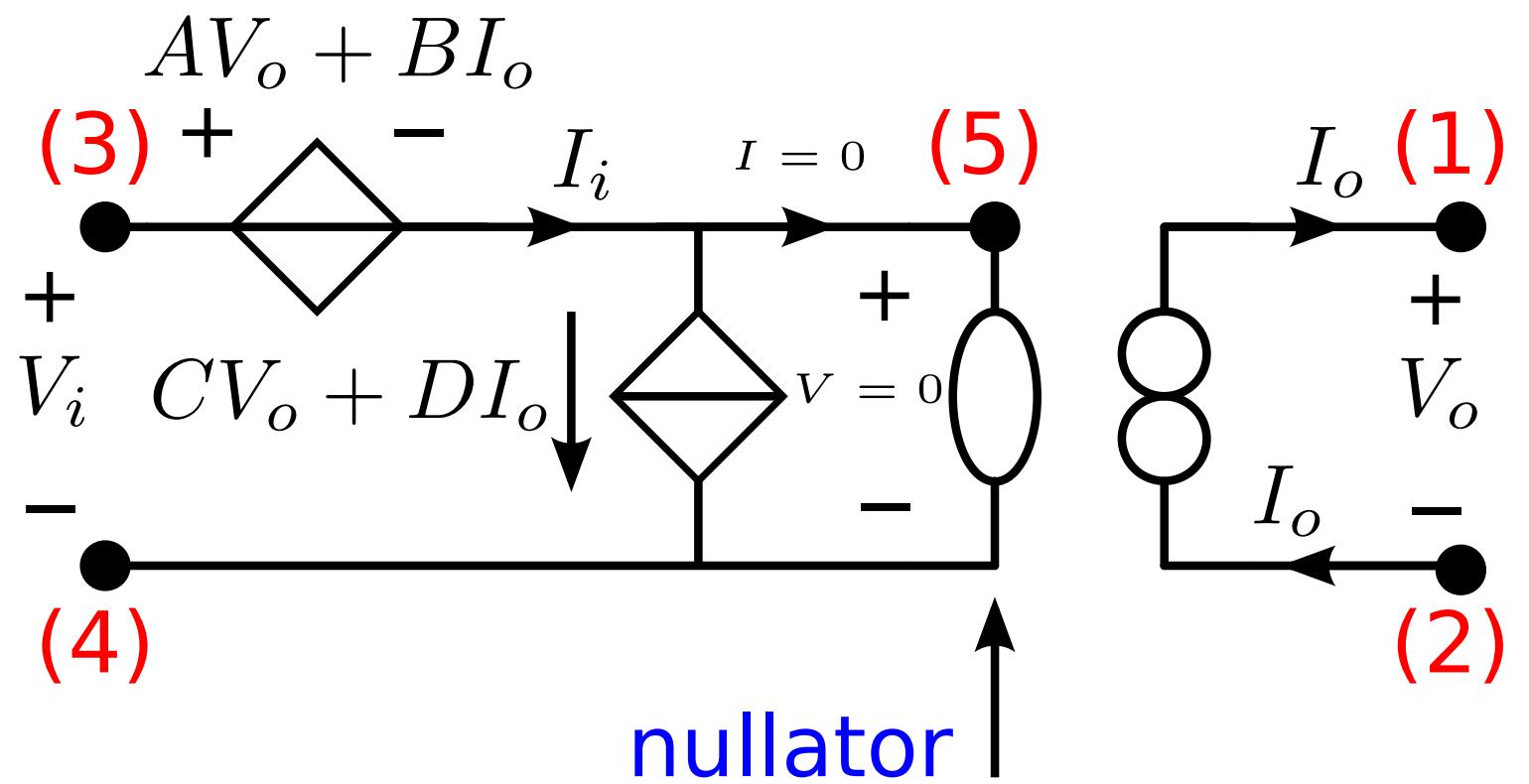
no	amplifier type	Z_i	Z_o	A	B	C	D
1	Voltage amplifier	∞	0	A	0	0	0
2	Transadmittance amplifier	∞	∞	0	B	0	0
3	Voltage input, finite nonzero output impedance	∞	Z_o	A	B	0	0
4	Transimpedance amplifier	0	0	0	0	C	0
5	Current amplifier	0	∞	0	0	0	D
6	Current input, finite nonzero output impedance	0	Z_o	0	0	C	D
7	Finite nonzero input impedance, voltage output	Z_i	0	A	0	C	0
8	Finite nonzero input impedance, current output	Z_i	∞	0	B	0	D
9	Finite nonzero input and output impedance	Z_i	Z_o	A	B	C	D

Generalized two-port model

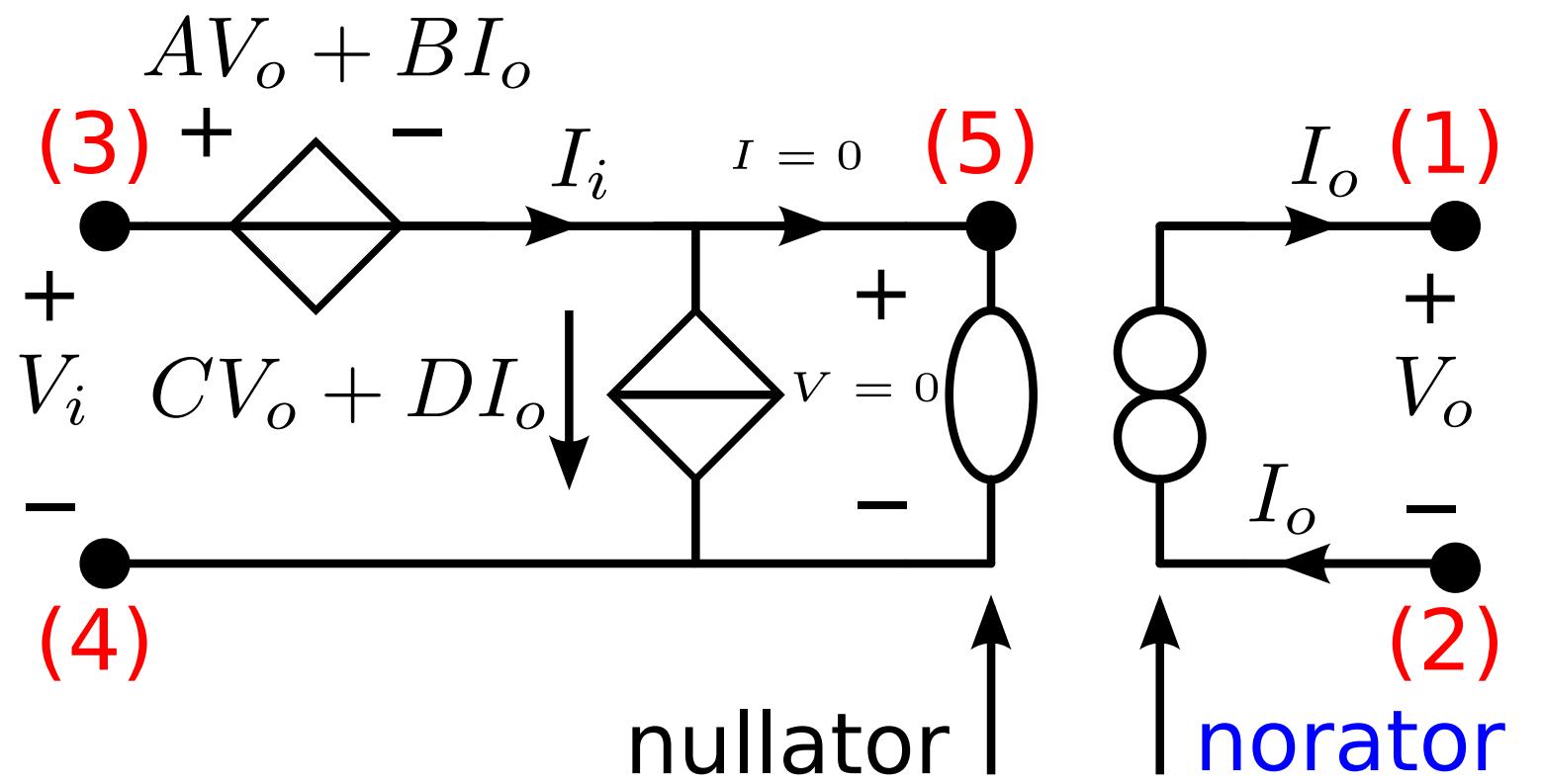
Generalized two-port model



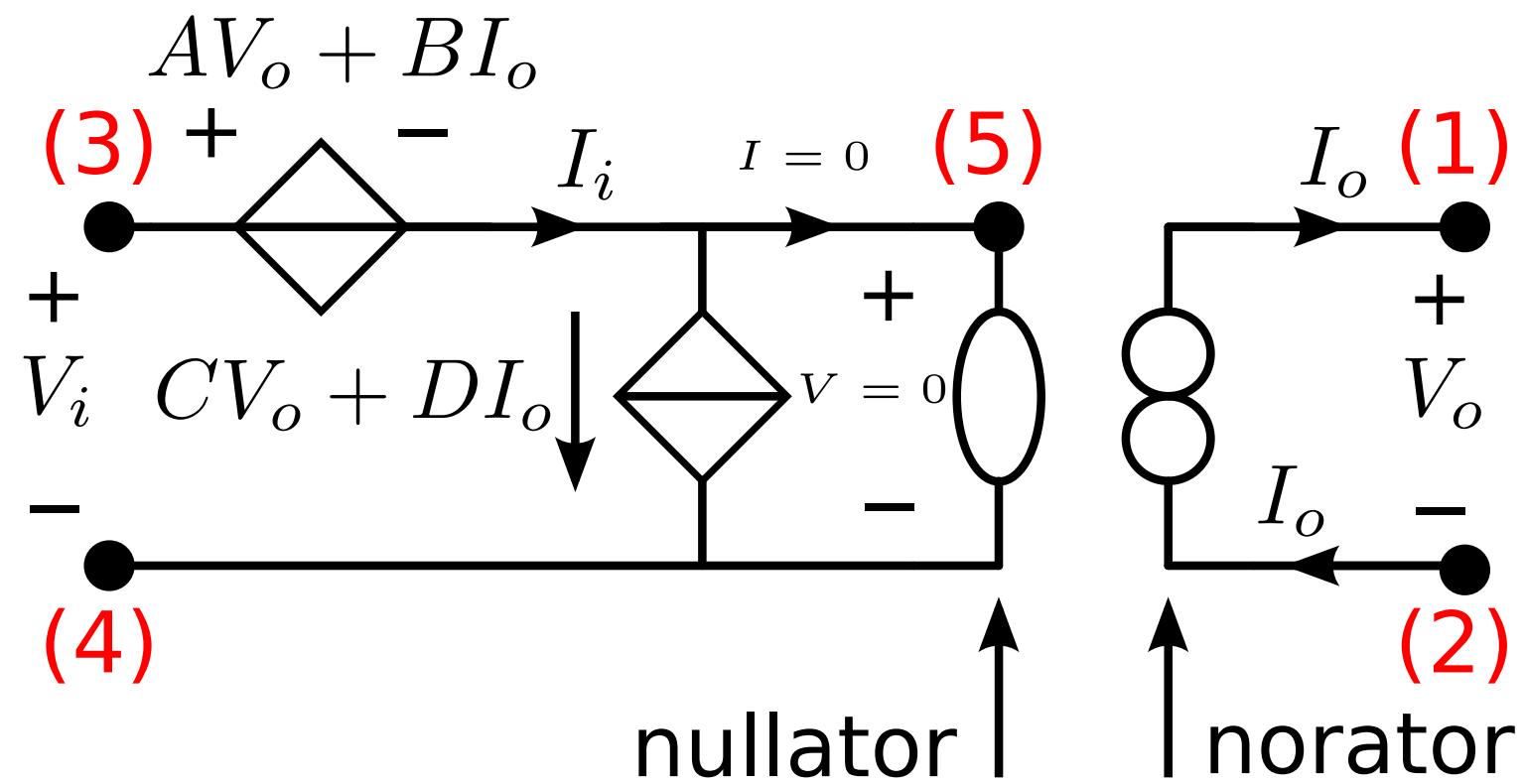
Generalized two-port model



Generalized two-port model

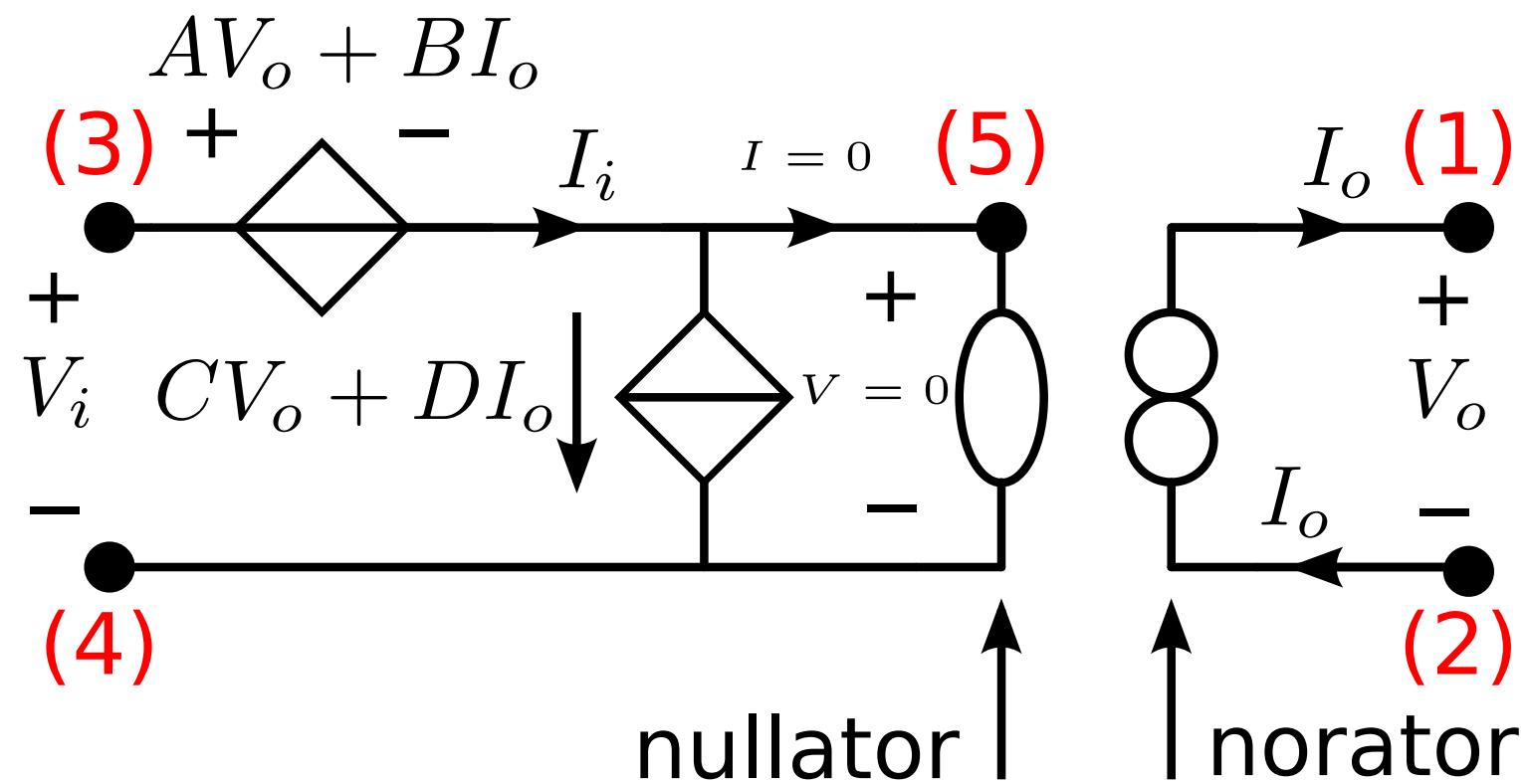


Generalized two-port model



Nullator and norator always
in pairs in a network
See section 18.3.3

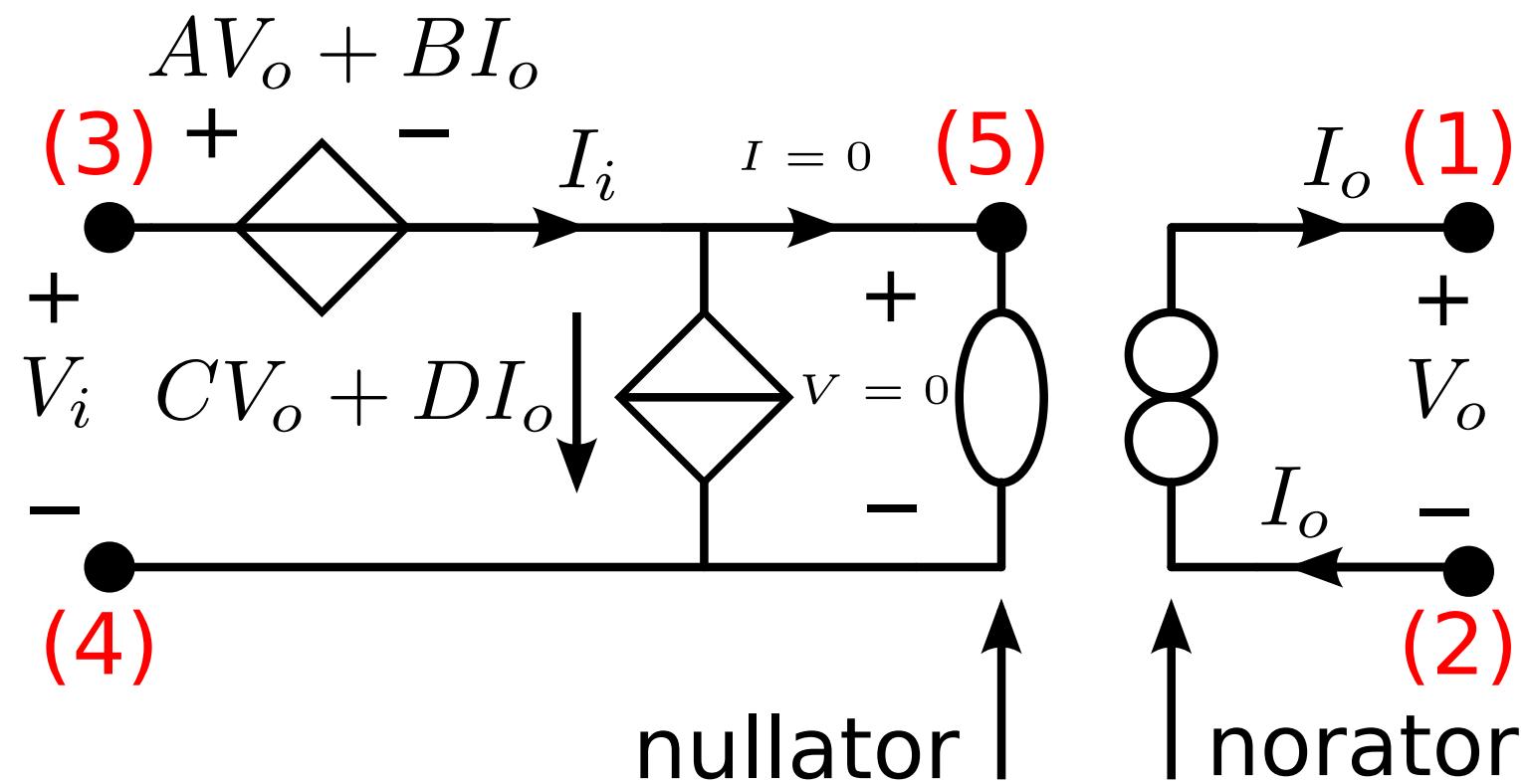
Generalized two-port model



Nullator and norator always
in pairs in a network
See section 18.3.3

Nullator sets network condition

Generalized two-port model

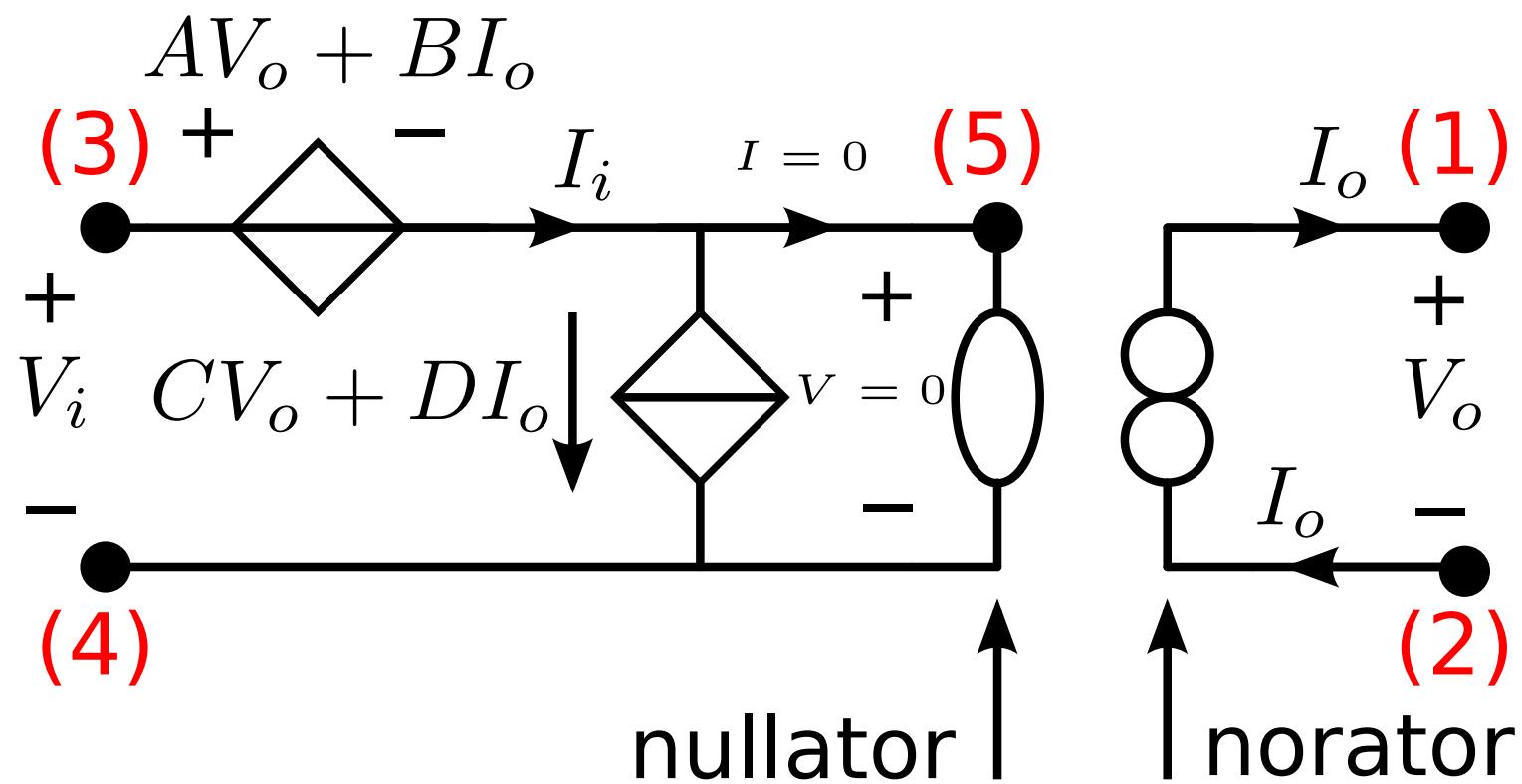


Nullator and norator always
in pairs in a network
See section 18.3.3

Nullator sets network condition

Norator adds variable

Generalized two-port model

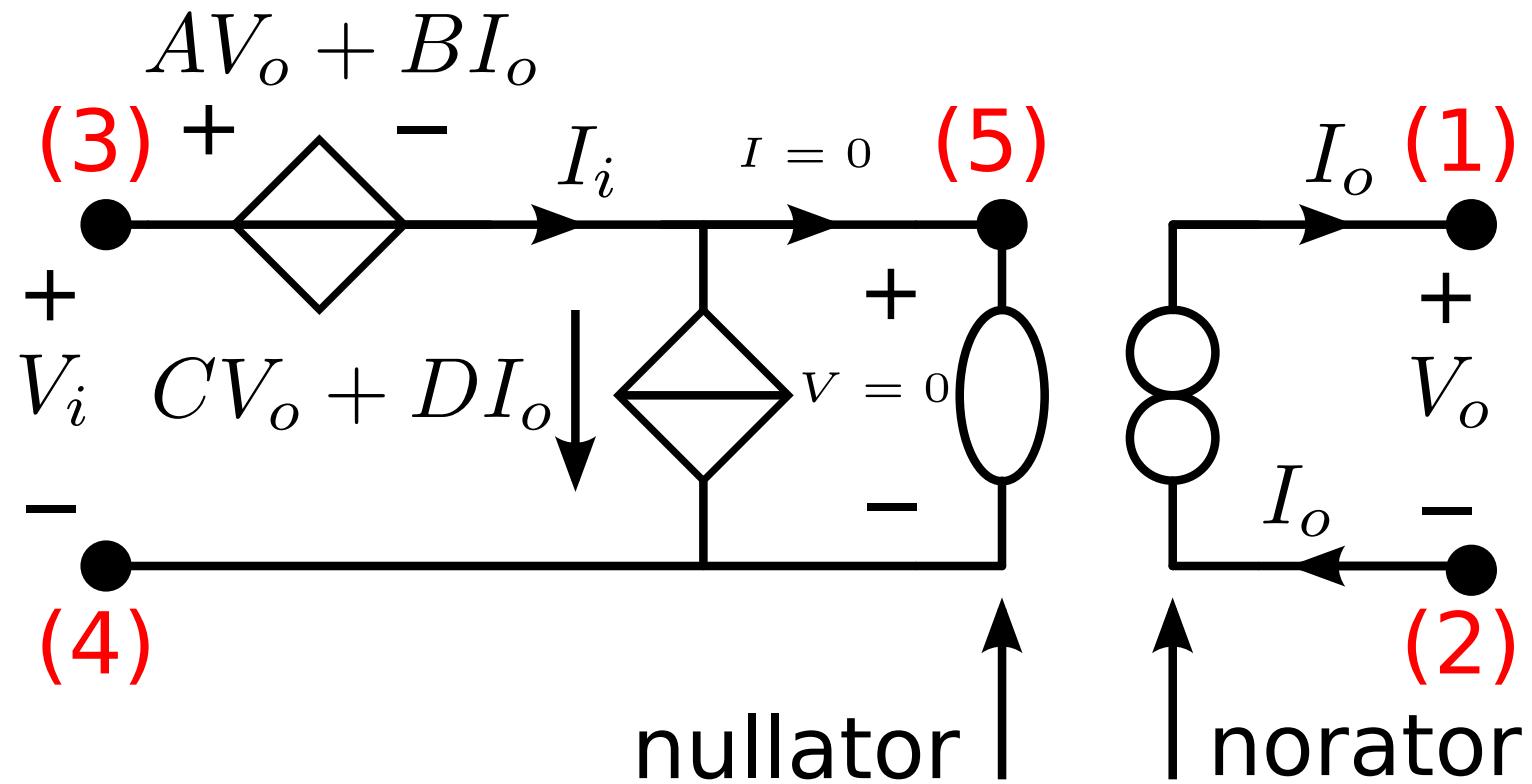


Nullator and norator always
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See section 18.3.3

Nullator sets network condition
Norator adds variable

Subcircuit included in SLiCAP: symbol SLABCD in LTspice.

Generalized two-port model



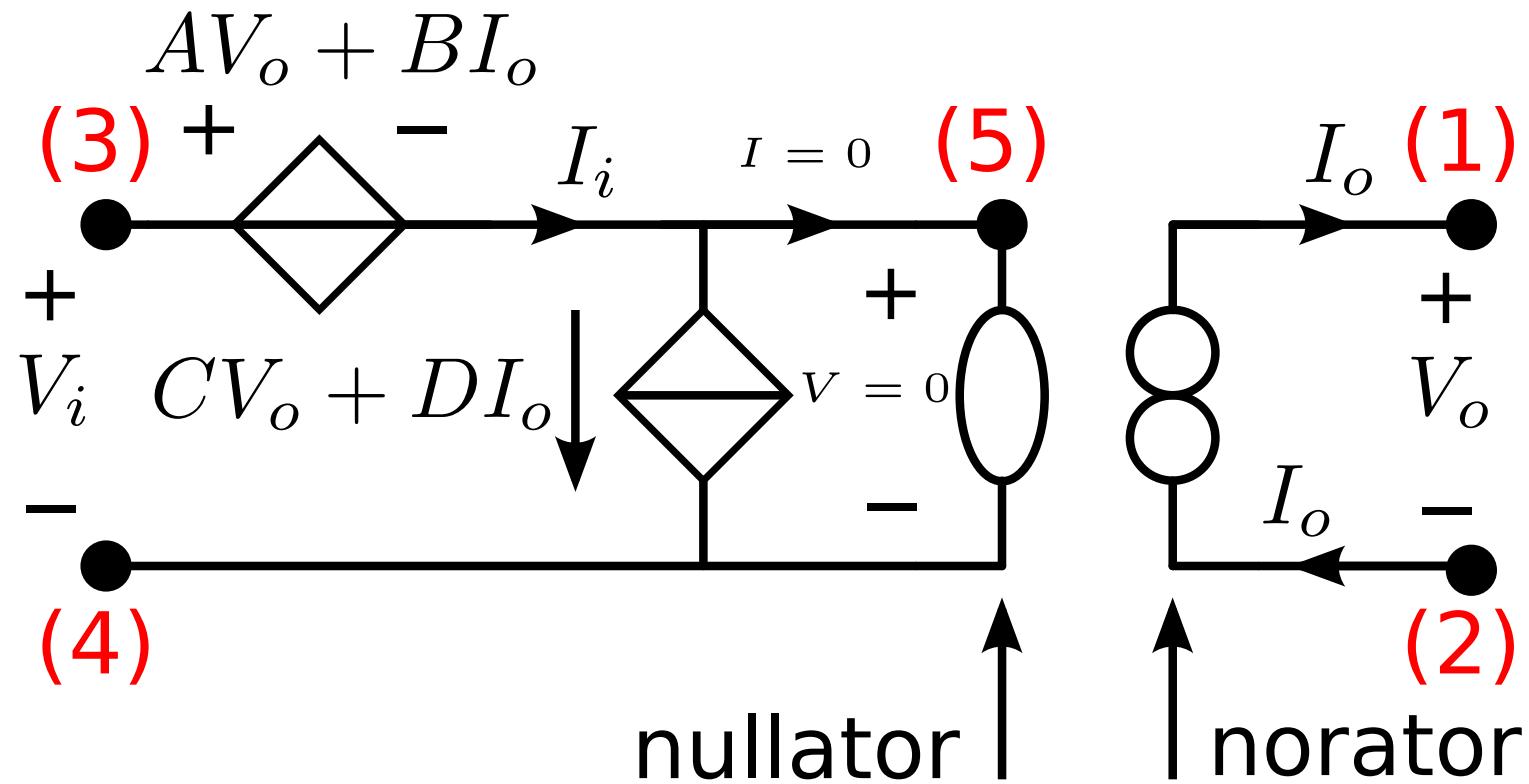
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Can only be used with $A, B, C, D = \text{Real}$

Generalized two-port model



Nullator and norator always
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