# **Structured Electronic Design**

Feedback model of Black

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## Invention of negative feedback

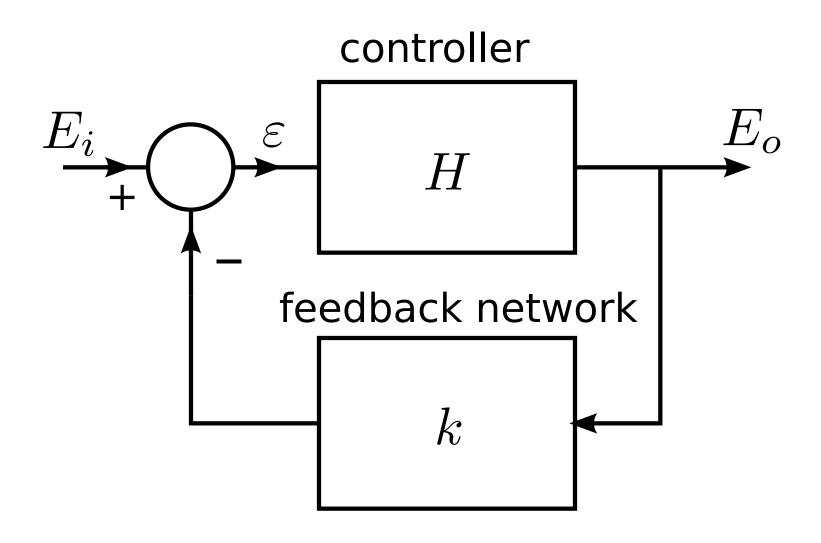
1927: Black: first negative feedback amplifier

1932: Black: Wave translation system

1932: Nyquist: Regeneration theory

1945: Bode: Network analysis and Feedback Amplifier Design

#### Black's feedback model



### **Equations:**

$$\varepsilon = E_i - kE_o,$$

$$\varepsilon = \frac{1}{H}E_o.$$

Input-output transfer:

$$\frac{E_o}{E_i} = \frac{H}{1+Hk}$$

loop gain: Hk

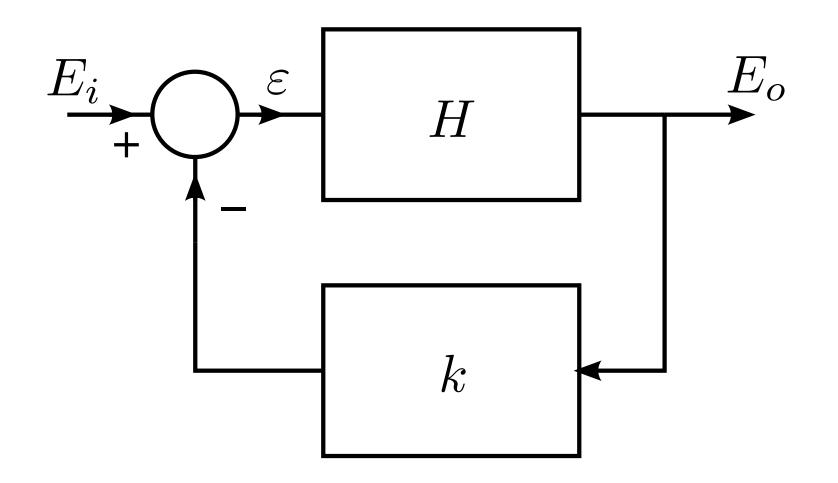
Ideal gain:  $Hk o \infty$ 

$$\lim_{Hk\to\infty} \left(\frac{E_o}{E_i}\right) = \frac{1}{k}$$

Input-output transfer, rewritten:

$$\frac{E_o}{E_i} = \frac{1}{k} \left( \frac{Hk}{1 + Hk} \right)$$

## Black's feedback model, assumptions



Ideal subtraction requires infinite CMRR, subtraction result does not depend on:

Source impedance

Input impedance controller

Output impedance feedback network

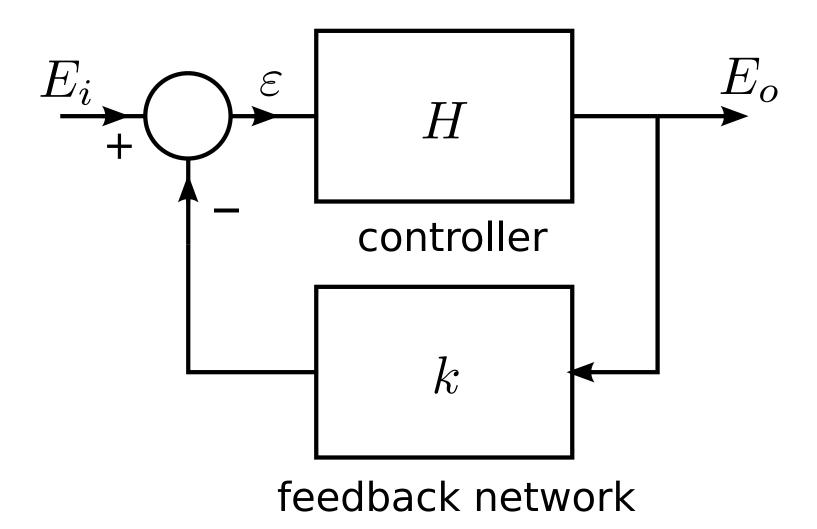
No direct transfer from input to output.

No reverse transfer in the controller and in the feedback network.

The controller gain does not depend on:

Input impedance feedback network Load impedance

### Black's feedback model, conclusions



Loop gain not simply the product of the controller gain (H) and the gain of the feedback network (k)

Suited for system-level analysis (no interaction between blocks)

Not suited for obtaining design information on circuit level

See example 10.1 and 10.2