Structured Electronic Design

EE3C11
Topics from Network Theory
Nodal Analysis

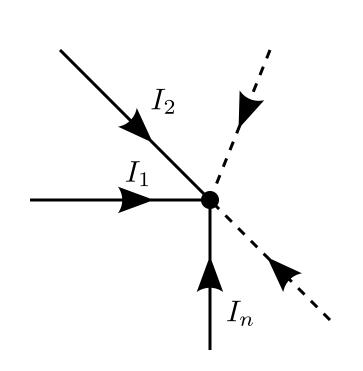
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Nodal Analysis

An electrical network consists of interconnected network elements

Node: interconnection point

Branch: element between two nodes



Kirchhoff's current law

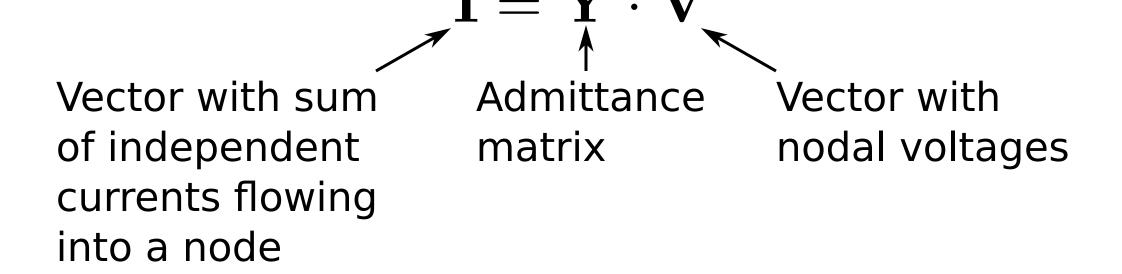
The sum of the branch currents that flow into (or from) a node, equals zero:

$$\sum_{i=1}^{i=n} I_i = 0$$

Network with n nodes

1 node selected as reference node n-1 nodal voltages w.r.t. voltage of ref. node n-1 independent nodal equations

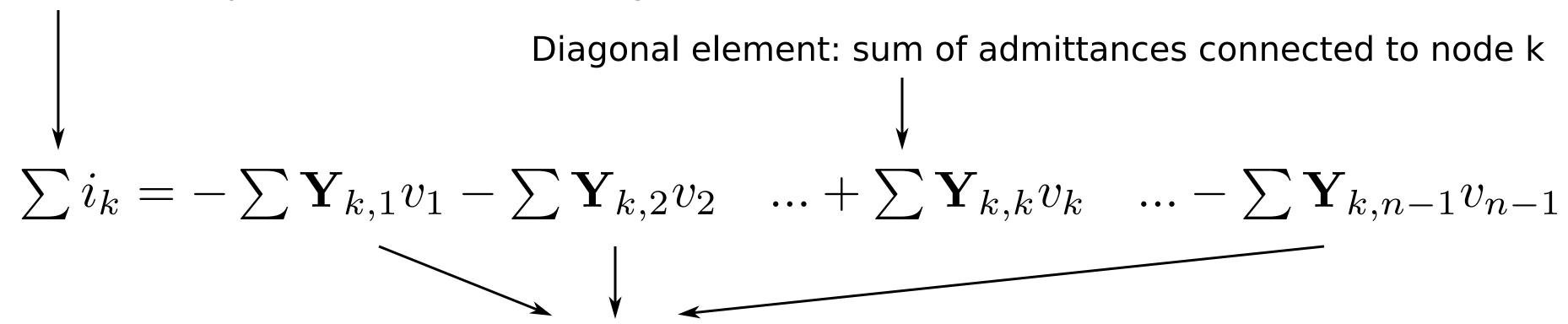
Only voltage-controlled elements: Branch current can be written as a function of the branch voltage



Admittance Matrix

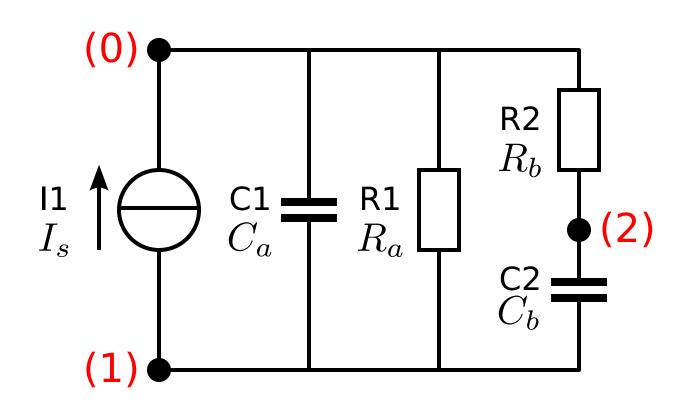
General form of nodal equation:

Sum of independent currents flowing into node k



Off-diagonal element: $\sum \mathbf{Y}_{k,j} = \text{Sum of admittances connected}$ between node k and node j

Nodal Analysis



Node (0) is reference node

Two independent nodal equations:

(1)
$$0 = I_s + V_1 sC_a + V_1 \frac{1}{R_a} + (V_1 - V_2)sC_b$$

(2)
$$0 = V_2 \frac{1}{R_b} + (V_2 - V_1)sC_b$$

In matrix form:

$$\begin{pmatrix} -I_s \\ 0 \end{pmatrix} = \begin{pmatrix} s\left(C_a + C_b\right) + \frac{1}{R_a} & -sC_b \\ -sC_b & sC_b + \frac{1}{R_b} \end{pmatrix} \begin{pmatrix} V_1 \\ V_2 \end{pmatrix}$$