Structured Electronic Design

EE3C11 Noise in Electronic Circuits Anton J.M. Montagne

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 In resistors $S_{V_n} = K rac{V_R^2}{f}$



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Equivalent circuit in which the voltage of V3 represents the total noise voltage



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Noise representation

- A noise-free two-port with two noise sources
- Six representations:
 4 port variables:
- * two independent variables
- * two dependent variables













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Can be translated into each other

- Example 2.9
- Example 19.2
- Measure spectrum of the output noise for open and shorted input

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Open input: Input noise voltage does not contribute to amplifier output noise





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Current split / redirect





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Equivalent two-port representations





Current split / redirect













































Design conclusions
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